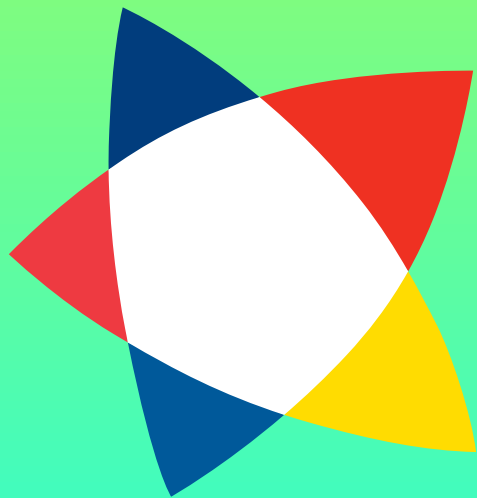


Multiband superconductivity in interface superconductors

Jonathan Edge
edge@kth.se

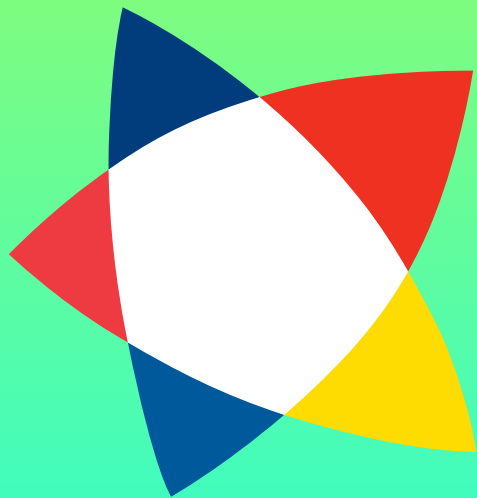


NORDITA

- Multiband superconductivity
- STO and LAO/STO
- Probes for multiband SC
- Multiband signature in H_{c2}
- Results for H_{c2} in STO and LAO/STO

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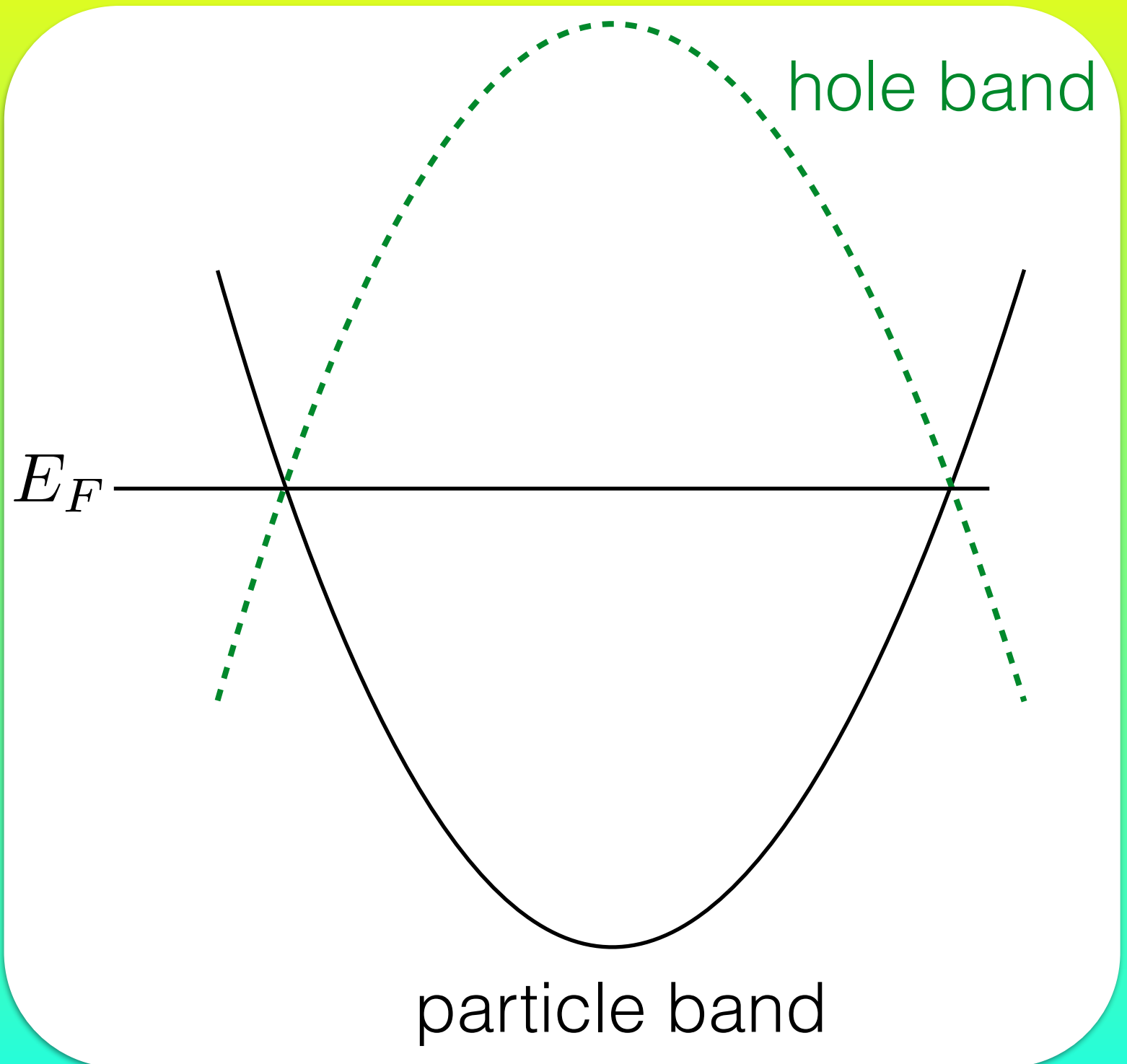


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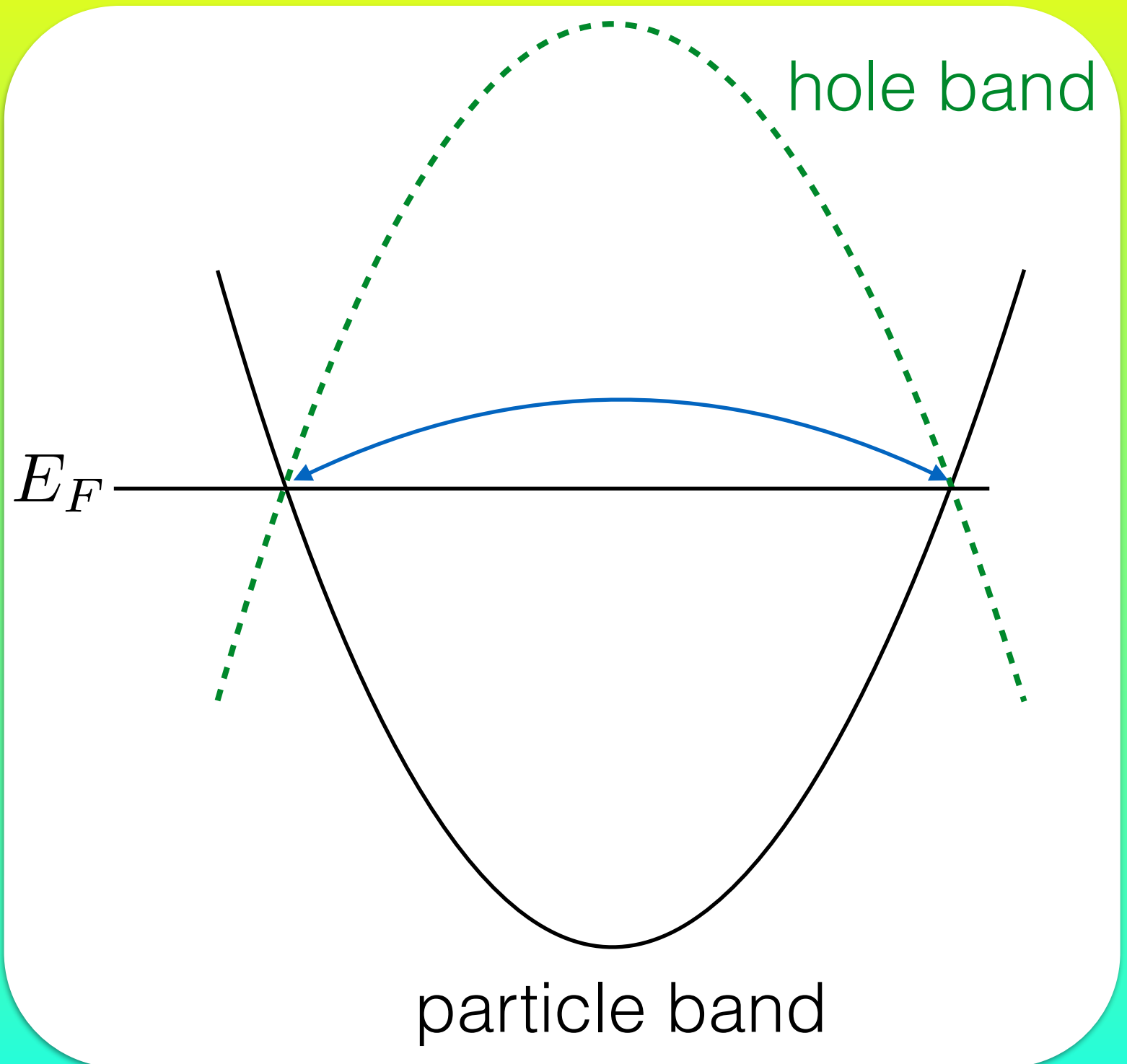
Ordinary single band superconductivity

- One band crossing Fermi energy
- Pairing between opposite sides of the Fermi surface opens a gap Δ in the density of states



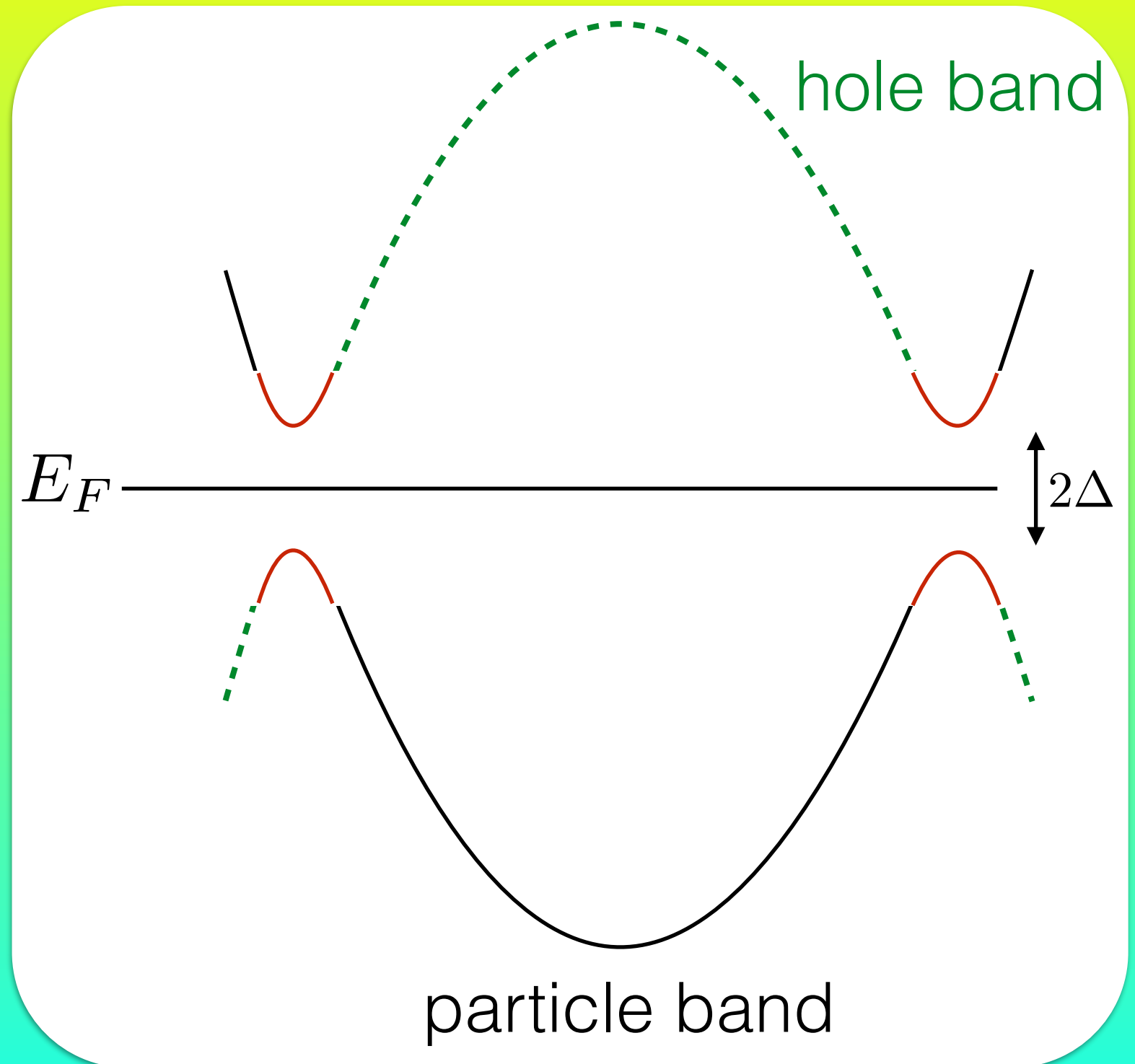
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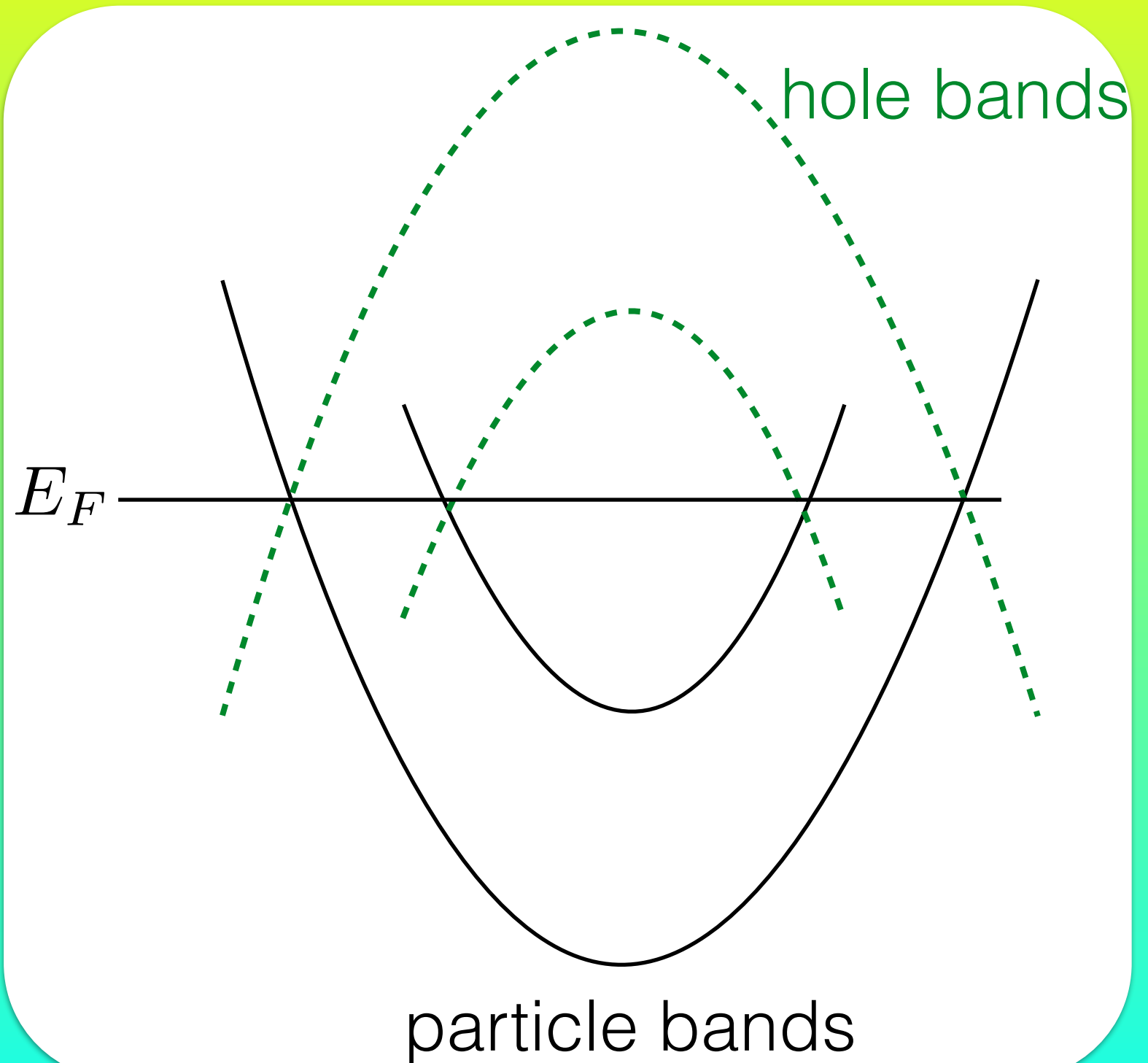
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Multiband superconductivity

Suhl, PRL 1959

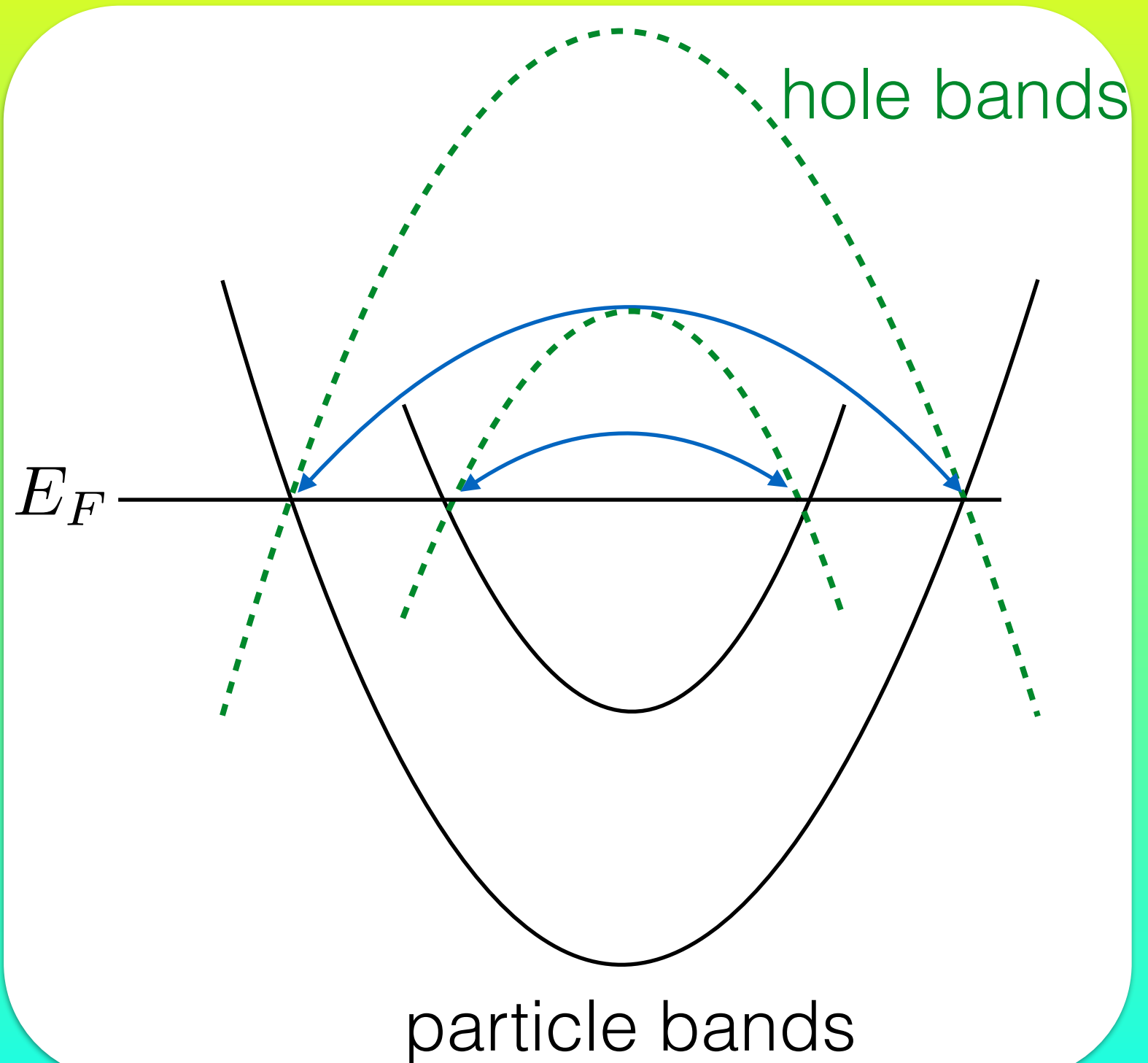
- Two bands crossing the Fermi energy
- Two (different) gaps Δ open up



Multiband superconductivity

Suhl, PRL 1959

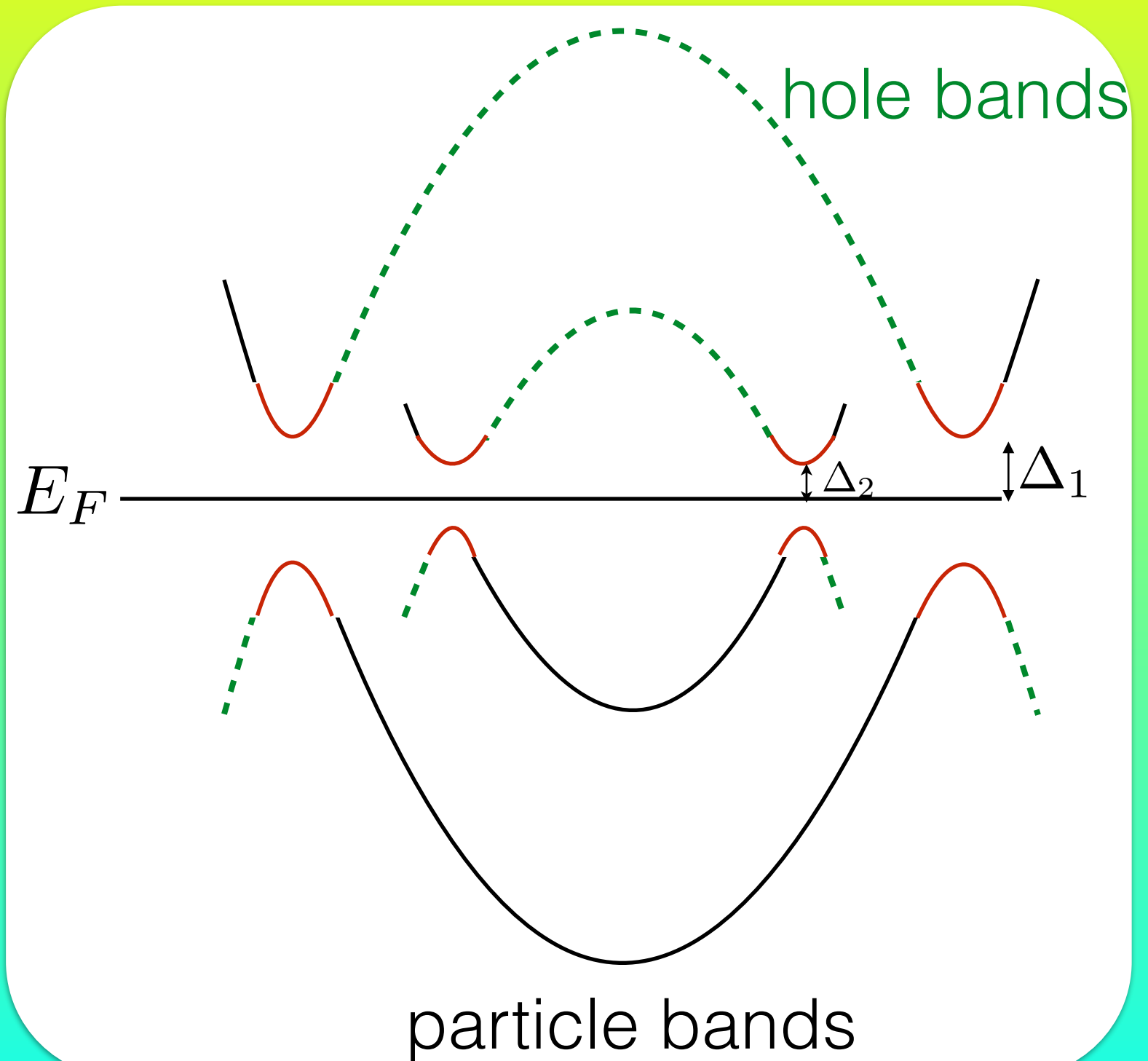
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Multiband superconductivity

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Multiband superconductivity

- Intrinsically interesting extension of superconductivity
- Allows for the interplay between the two gaps, novel dynamics
- Increasing number of materials are found to be multiband superconductors

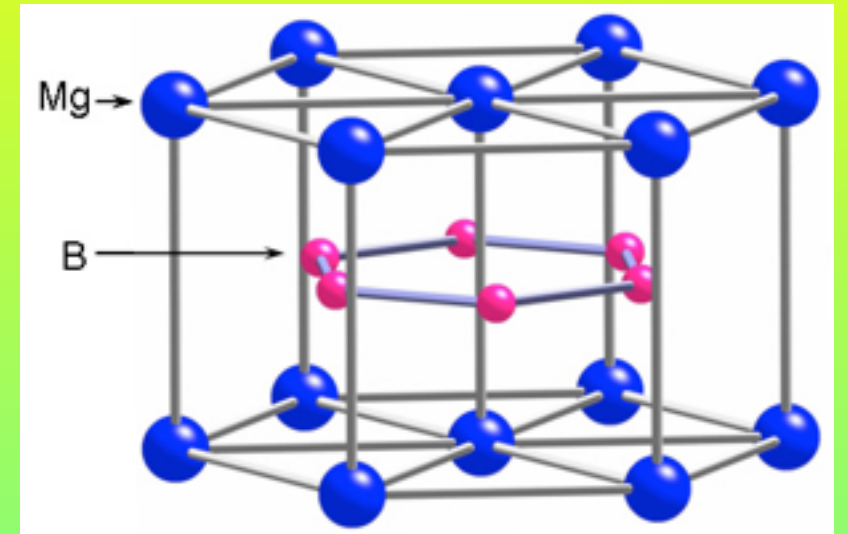
Multiband superconductivity

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Our interest: is the specific material SrTiO_3 (STO) and the interface between LaAlO_3 (LAO) and STO a multiband superconductor?

Examples of Multiband SCs

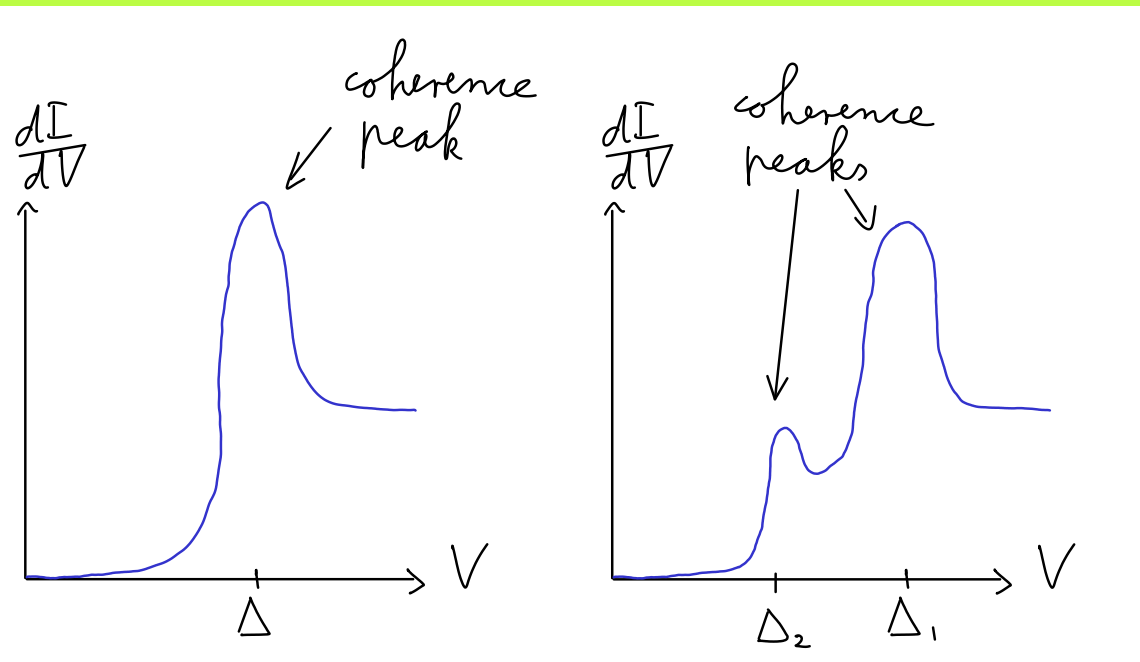
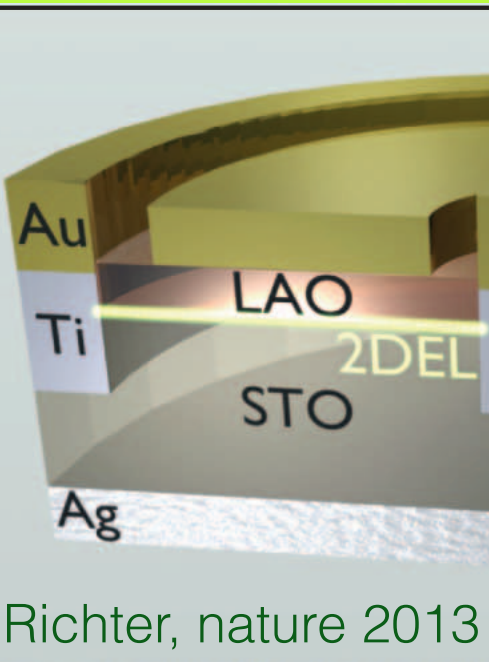
- MgB₂ (2001)
- Fe based superconductors (2008)
- various heavy fermion SCs
(PrOs₄Sb₁₂ (2005), CePt₃Si ,
Seyfarth, PRL 2005 Mukuda, JPSJ 2009
uranium compounds...)



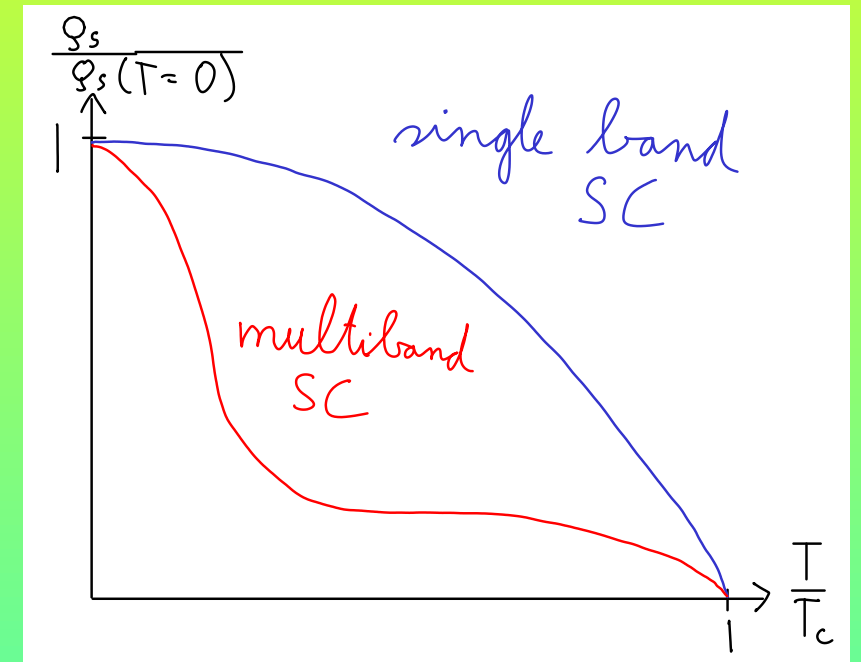
Nagamatsu, J. et al., 2001

Detecting Multiband SC

- Tunnelling spectroscopy: multiple coherence peaks



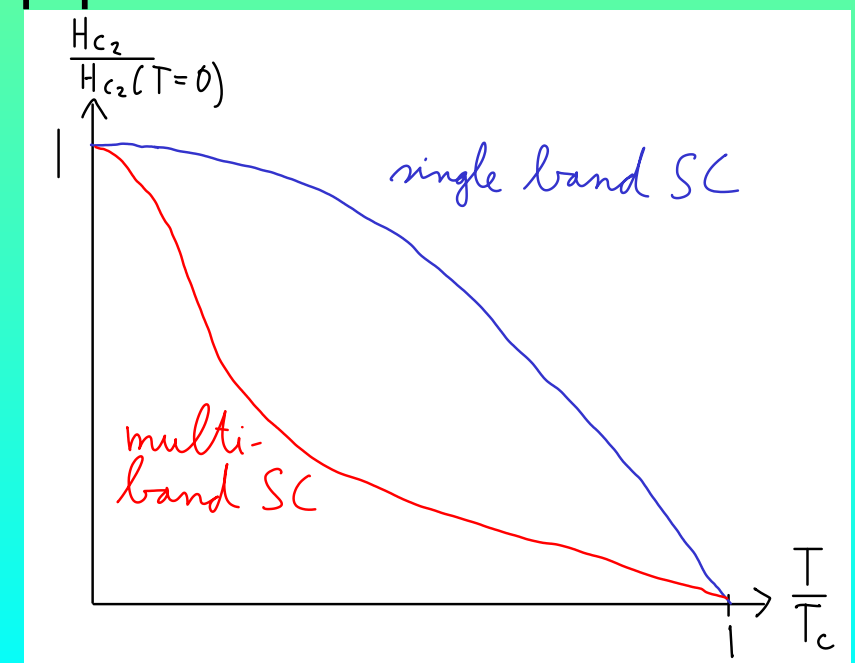
- superfluid density



- Heat transport

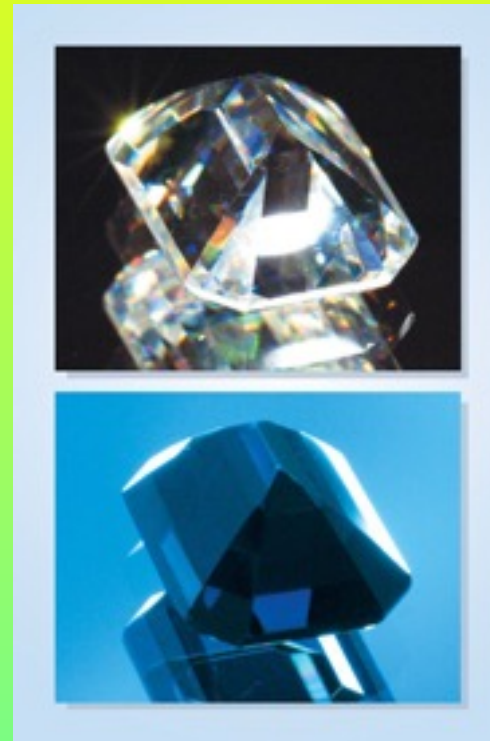


- upper critical field

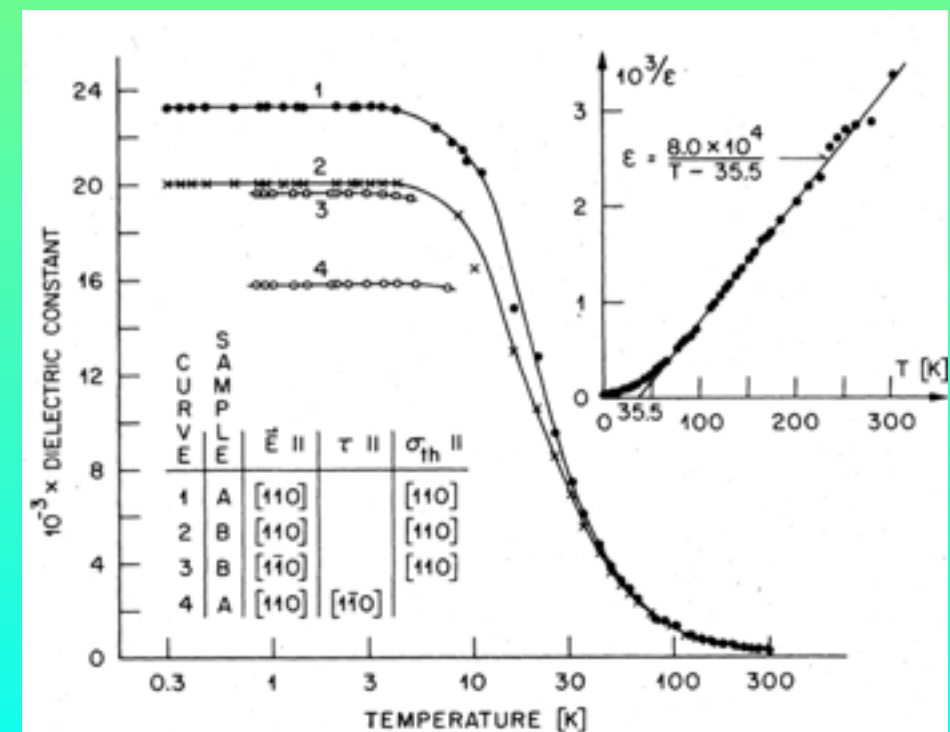


Strontium Titanate (STO)

- Wide bandgap insulator, bandgap $\sim 3\text{eV}$
- Doping with Nb, La or oxygen vacancies make it conducting
- Ferroelectric instability - nearly developed
- Has been studied experimentally and theoretically for 50 years



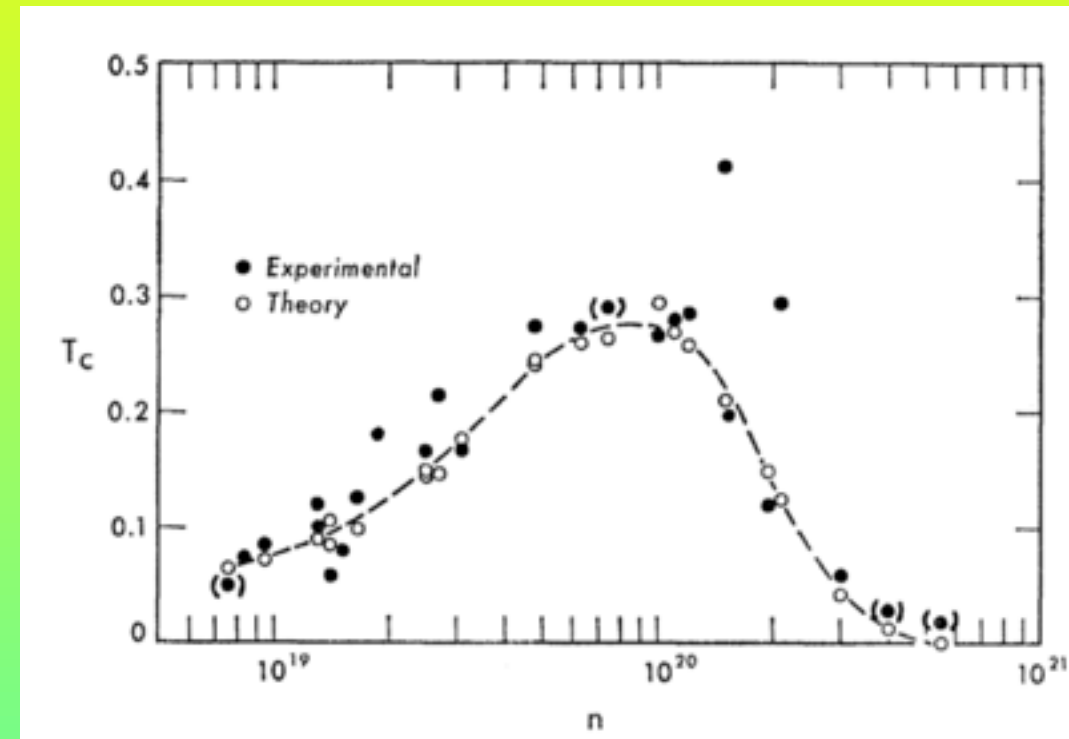
Mannhart, Nature 2004



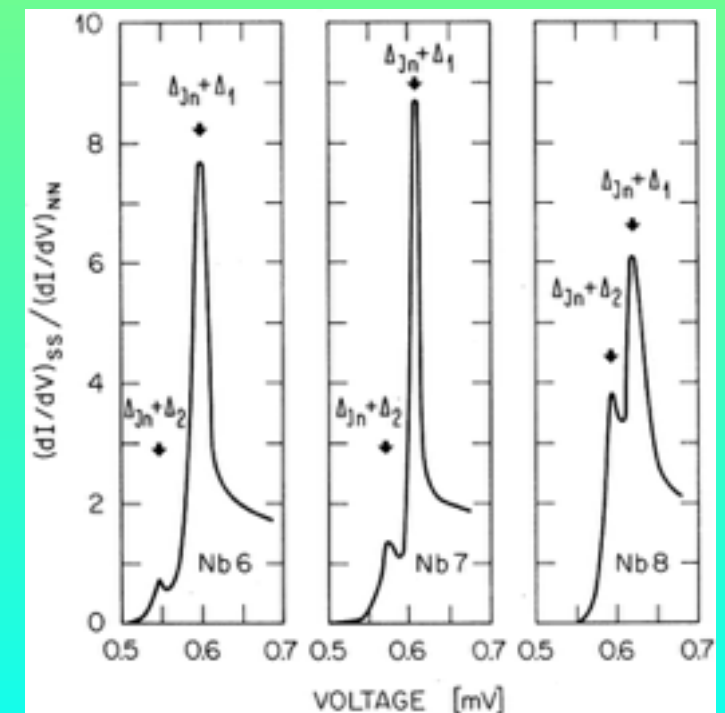
Müller, PRB (1979)

Superconductivity in STO

- First oxide superconductor to be discovered
- Doping-tunable SC dome
- Inspired the search which resulted in high T_c cuprate SC
- First material discovered to be a multiband superconductor



Koonce et al PR 163 380

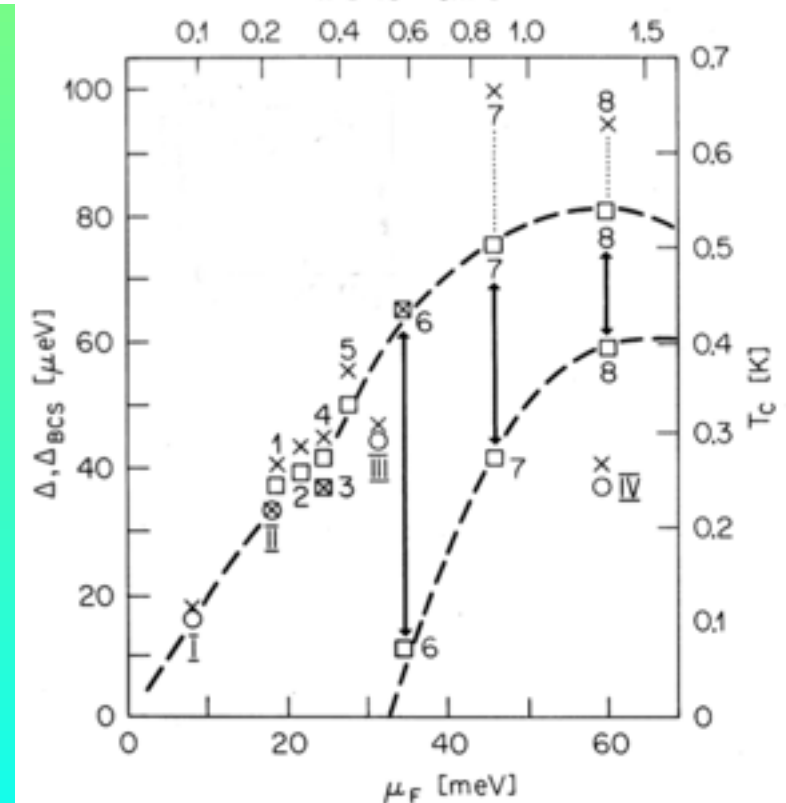
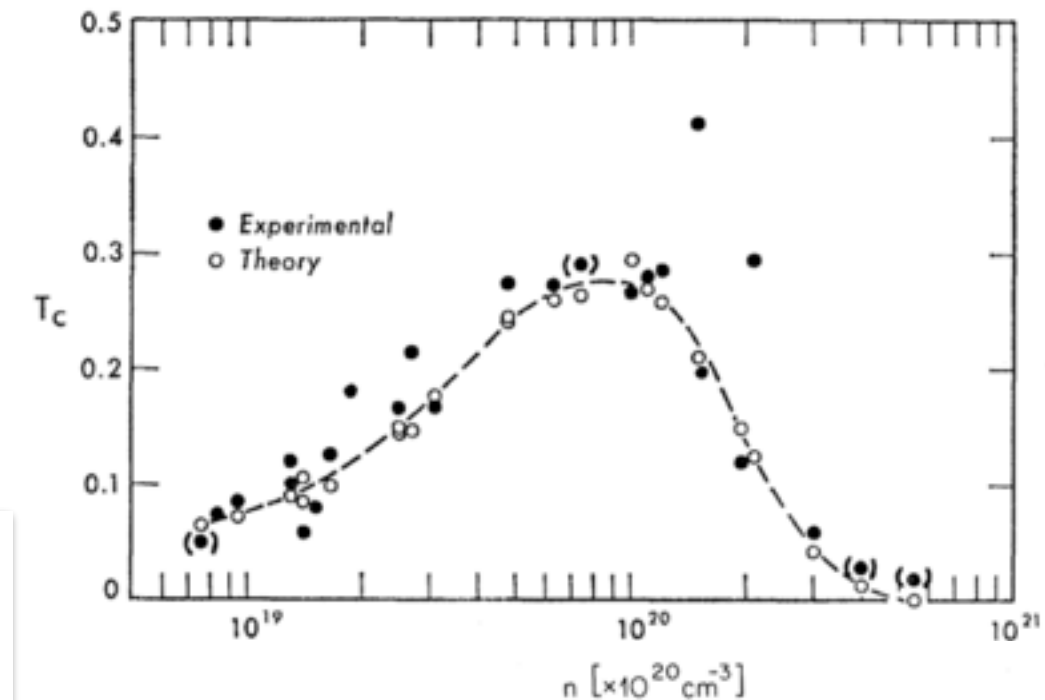
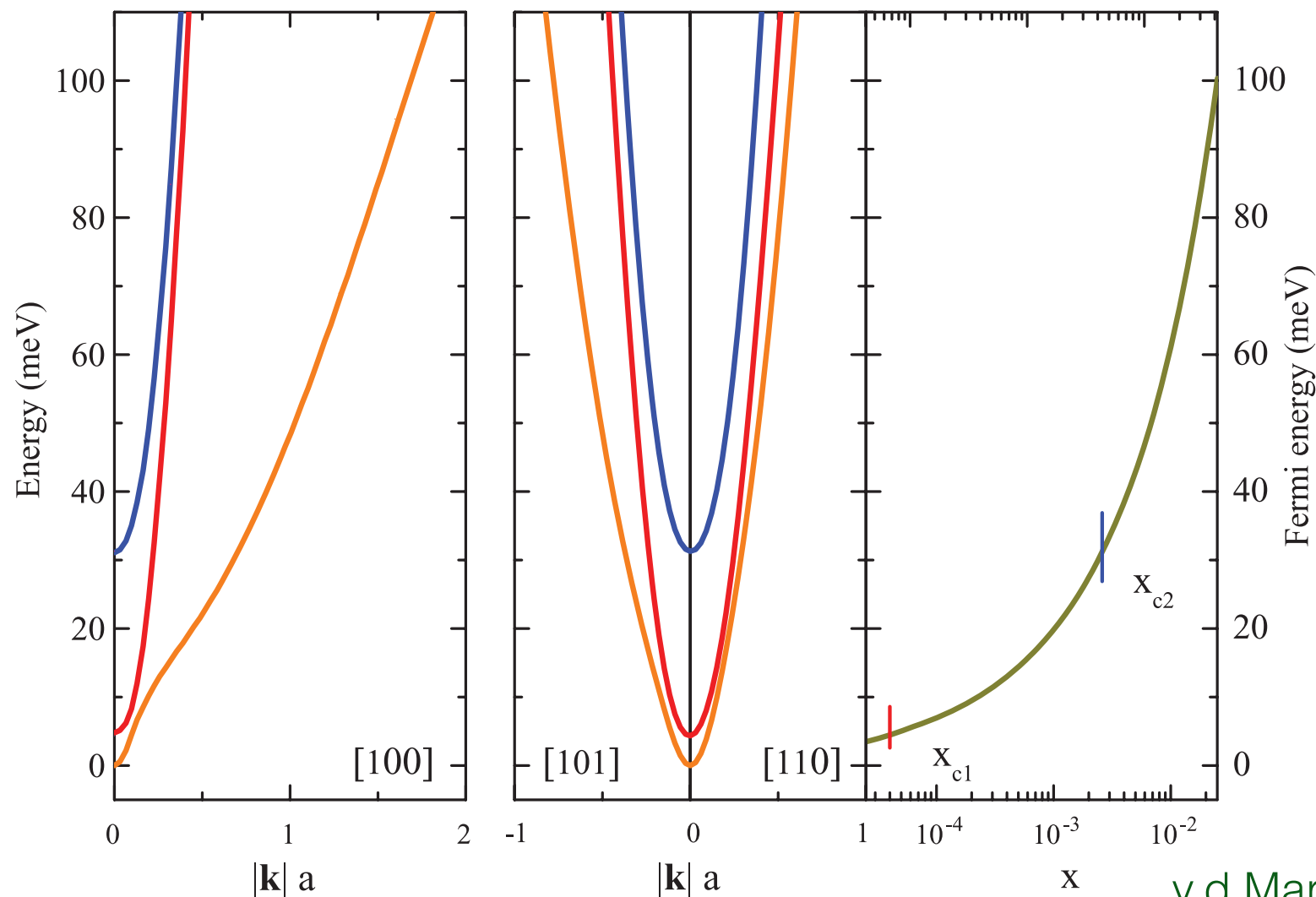


v.d.Marel, PRB 2011

Binnig, PRL1980

Superconductivity in STO

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LAO/STO interface

- Like STO, LaAlO_3 (LAO) is also an insulator (band gap $\sim 5\text{eV}$)
- But: when interface pure STO and LAO find a metallic interface layer

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STO

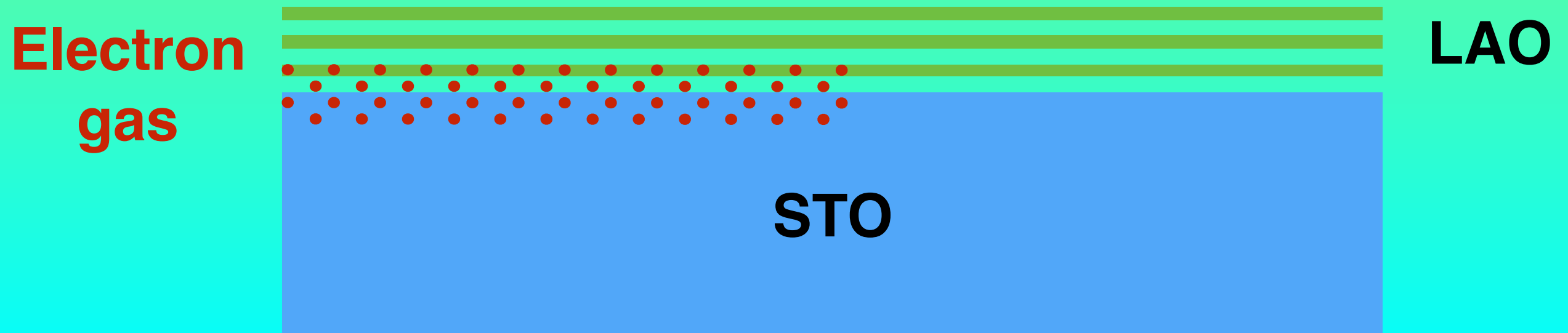
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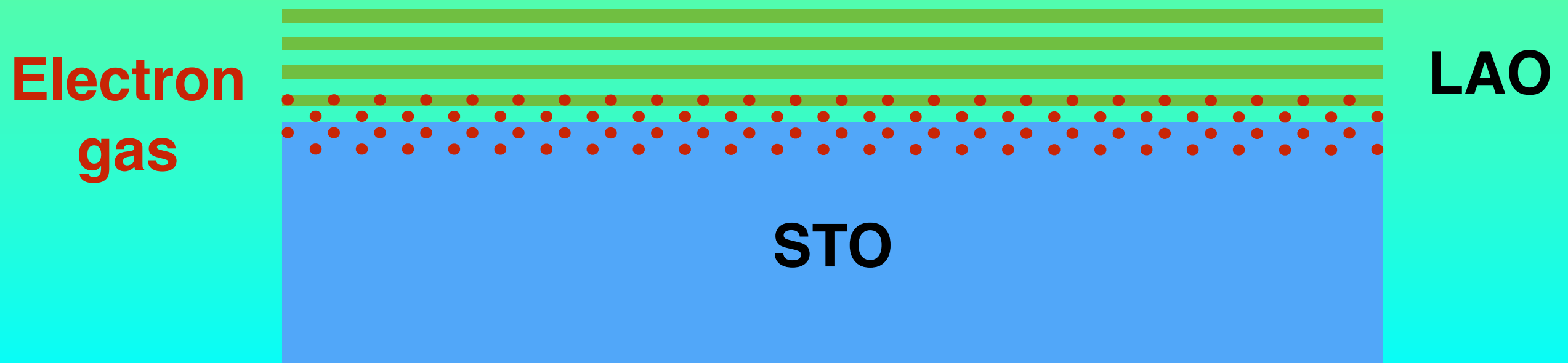
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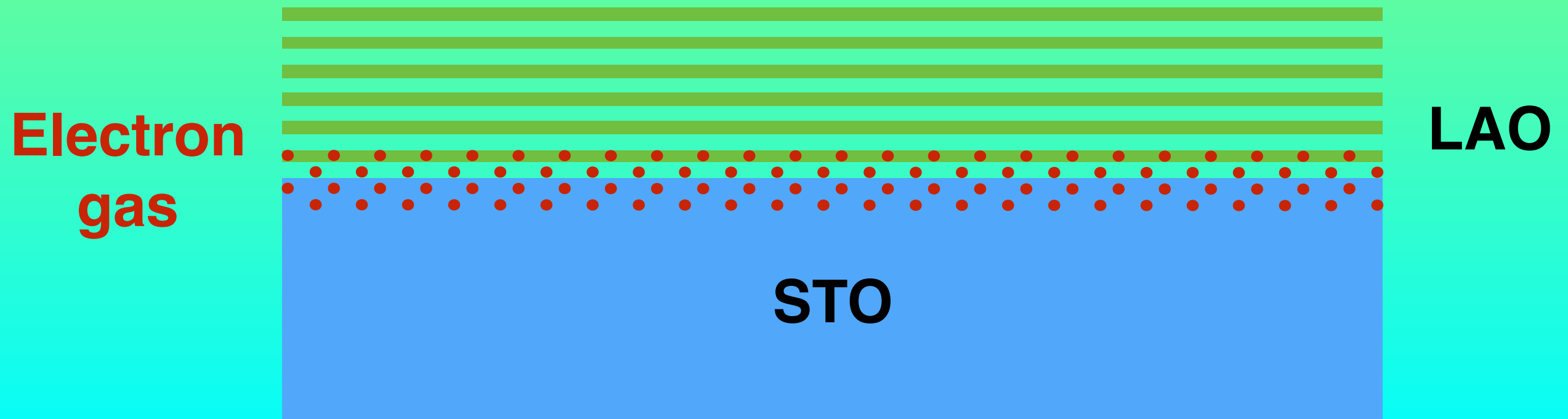
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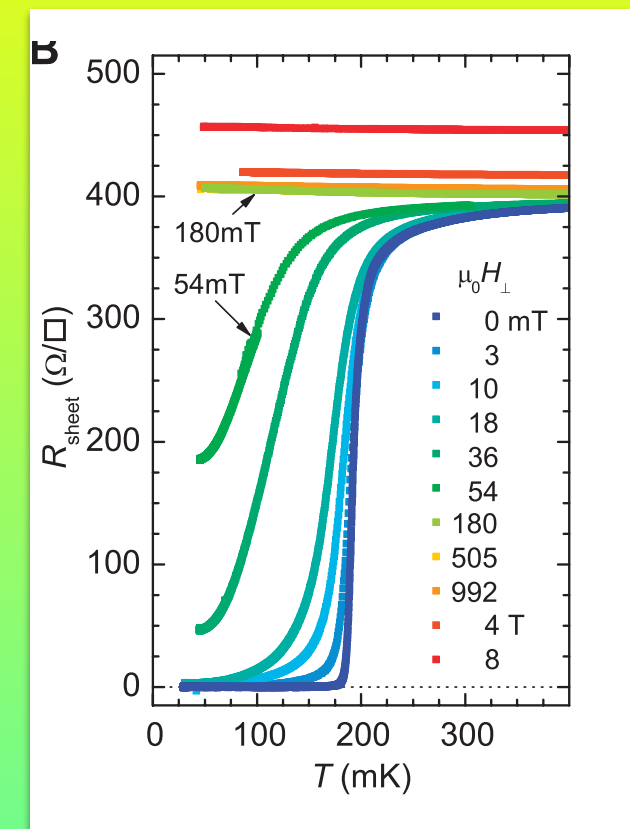
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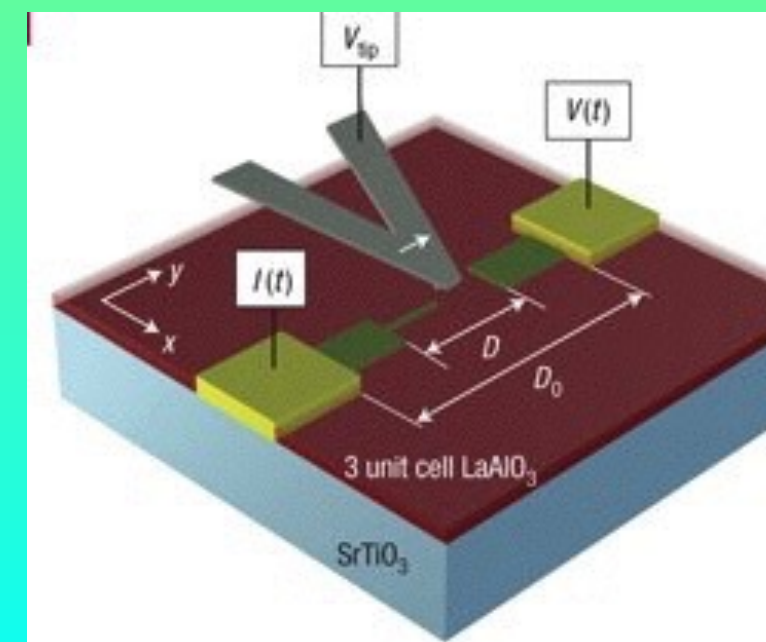


Superconductivity at the LAO/STO interface

- Metallic layer turns superconducting at low T
- For 3 layers of LAO, STM superconducting areas can be patterned with STM on nm scale
- Holds the promise for SC circuits and devices



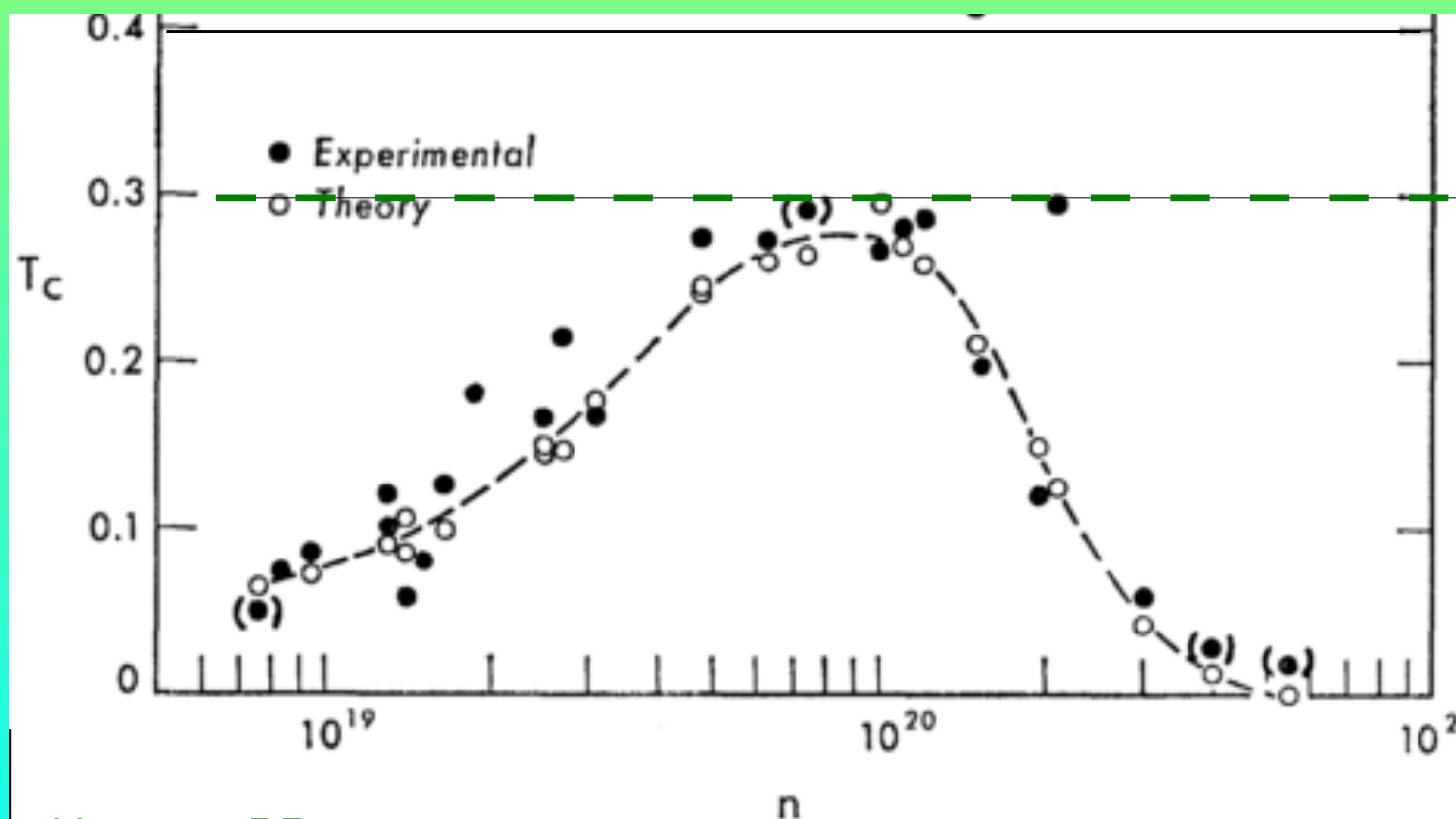
Reyren, Science 2007



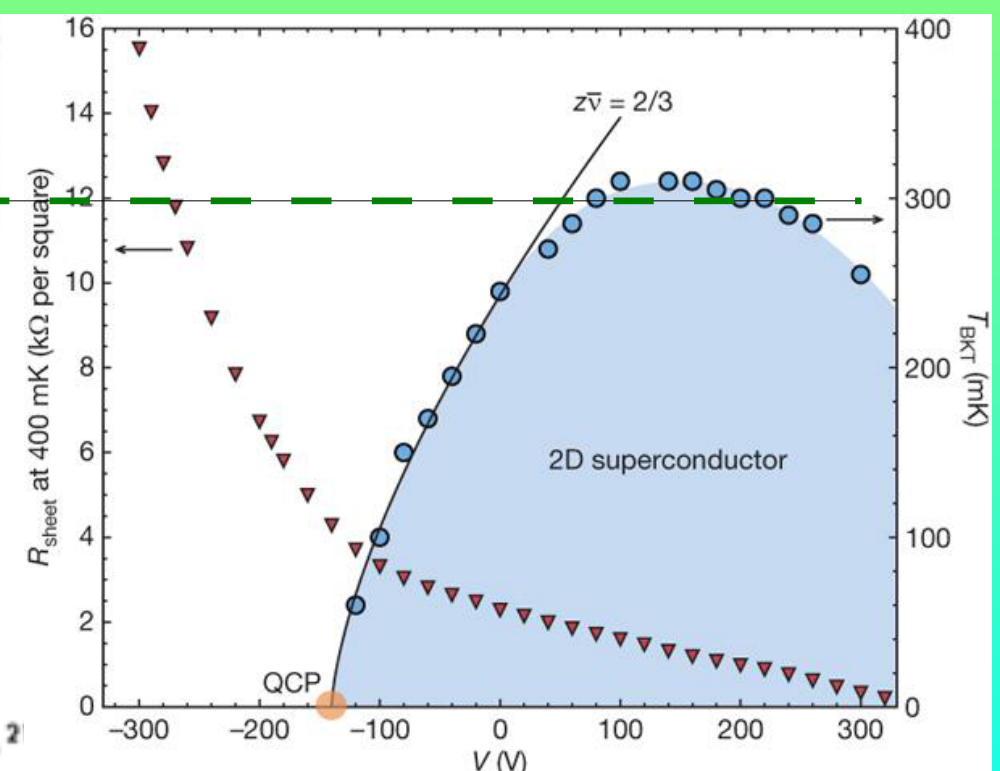
Cen, Nat. Mat. 2008

Central question: What is the relation between bulk and interface STO?

- T_c is similar ($\approx 300\text{mK}$), robust to quality variations of the sample/interface material
- As a function of doping/gate voltage a narrow superconducting dome appears.



Koonce PR 1967

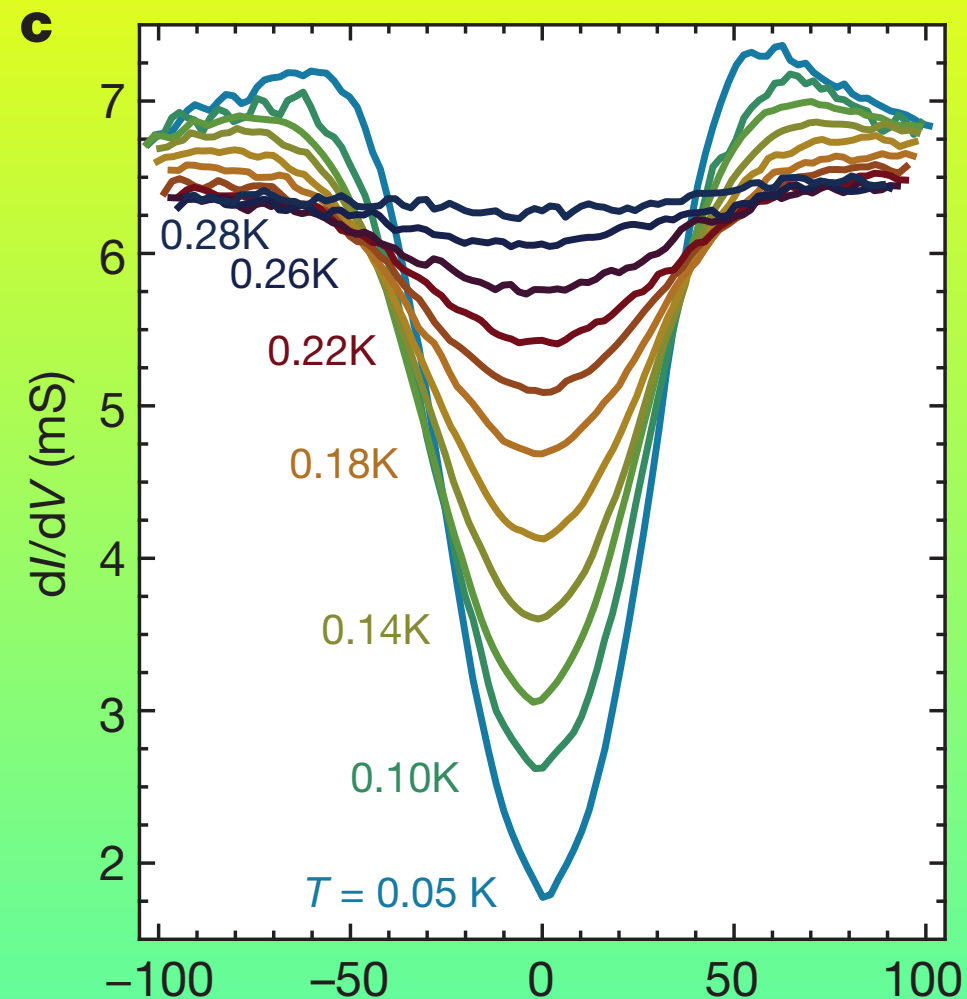


Cavaglia Nature 2008

Is LAO/STO a multiband SC, like STO?

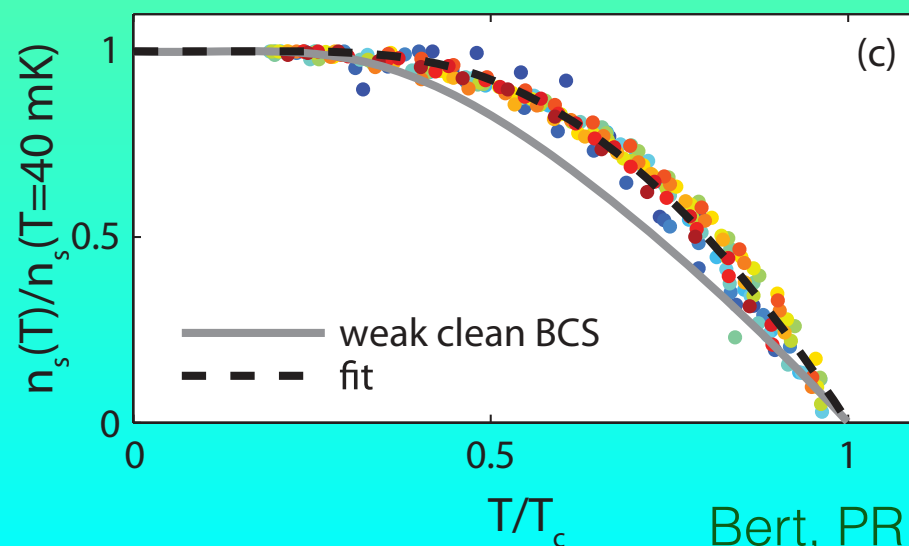
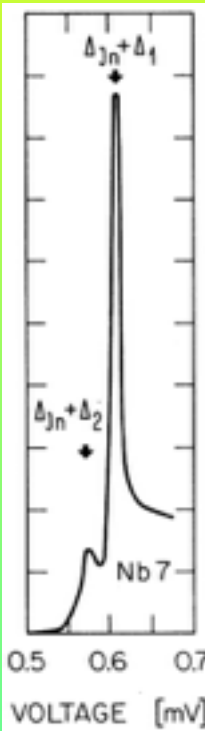
Probes which have tried to address this issue

- Tunnelling spectroscopy
- Superfluid density



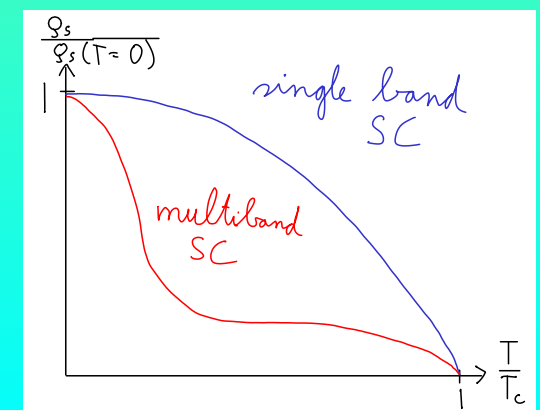
Richter, Nature 2013

compare
STO



Bert, PRB 2012

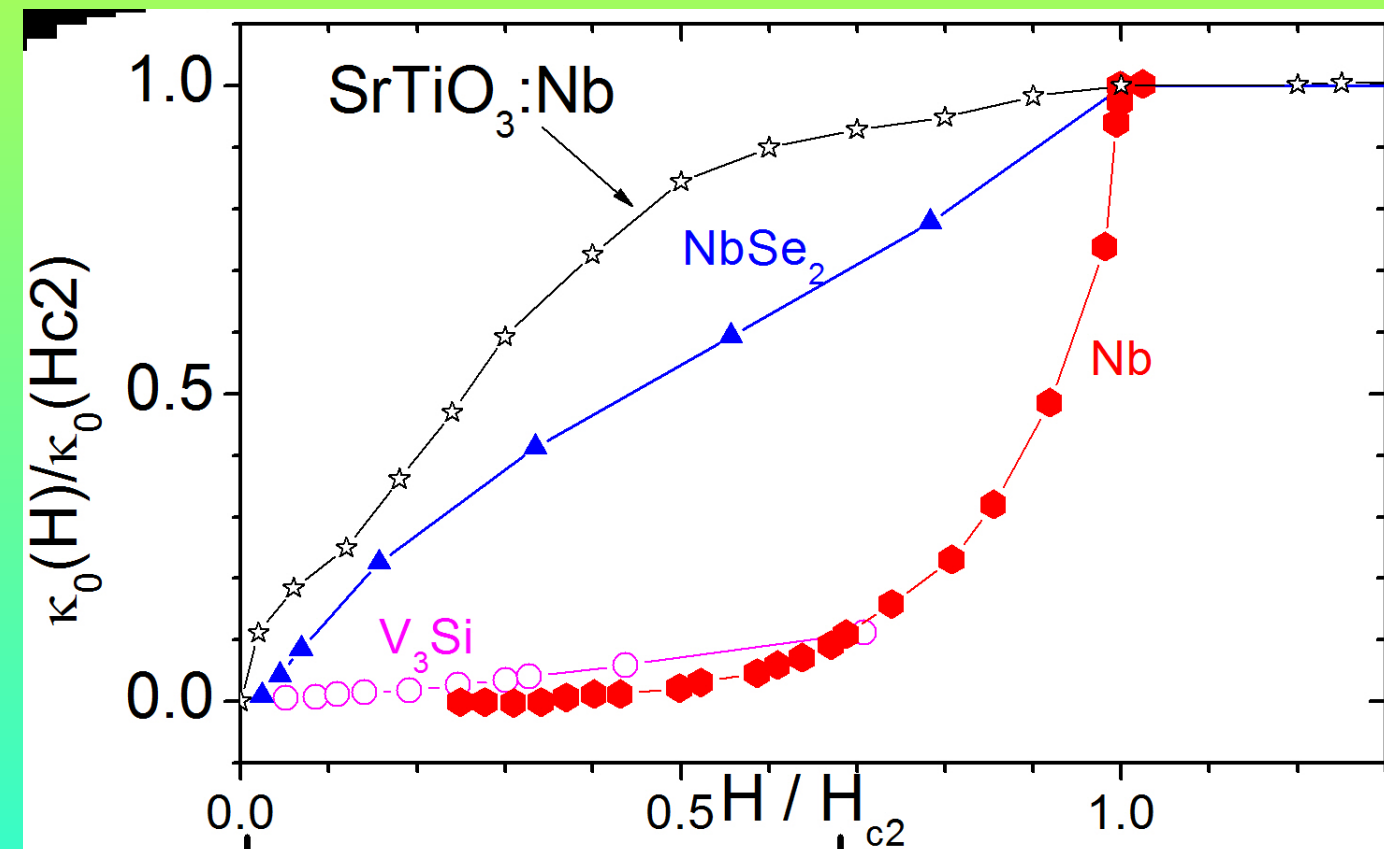
compare



Is LAO/STO a multiband SC, like STO?

Other potential probes

- Heat transport
- Heat capacity
- impractical for interface



Suggest looking at the upper critical field H_{c2} as a probe for multiband superconductivity in LAO/STO

H_{c2} as a probe for multiband SC in LAO/STO and STO

H_{c2} is one of the few probes applicable both to the bulk and interface system

- Calculate expected H_{c2} behaviour for both bulk and interface
- Show characteristic multiband behaviour
- Allows direct comparison of bulk and interface system

Disordered bulk STO: quasiclassical Usadel equations

- Solve linearised Usadel equations with a B-field $H \parallel \hat{z}$.

$$2\omega f_m - D_m \left(\nabla_x^2 + \nabla_y^2 + \nabla_z^2 + \frac{4\pi i H x}{\phi_0} \nabla_y - \frac{4\pi^2 H^2 x^2}{\phi_0^2} \right) f_m = 2\Delta_m$$

m : band index ($\in \{1, 2\}$),

D_m : Diffusion coefficient in the band

f_m : quasiclassical anomalous Green's function

- Linearised: valid for infinitesimal gaps Δ , so at T_c .
- 2-band gap equation:

$$\Delta_m = 2\pi T \sum_{\omega > 0}^{w_D} \sum_{m'} \lambda_{mm'} f_{m'}(\vec{r}, \omega)$$

λ : coupling constants

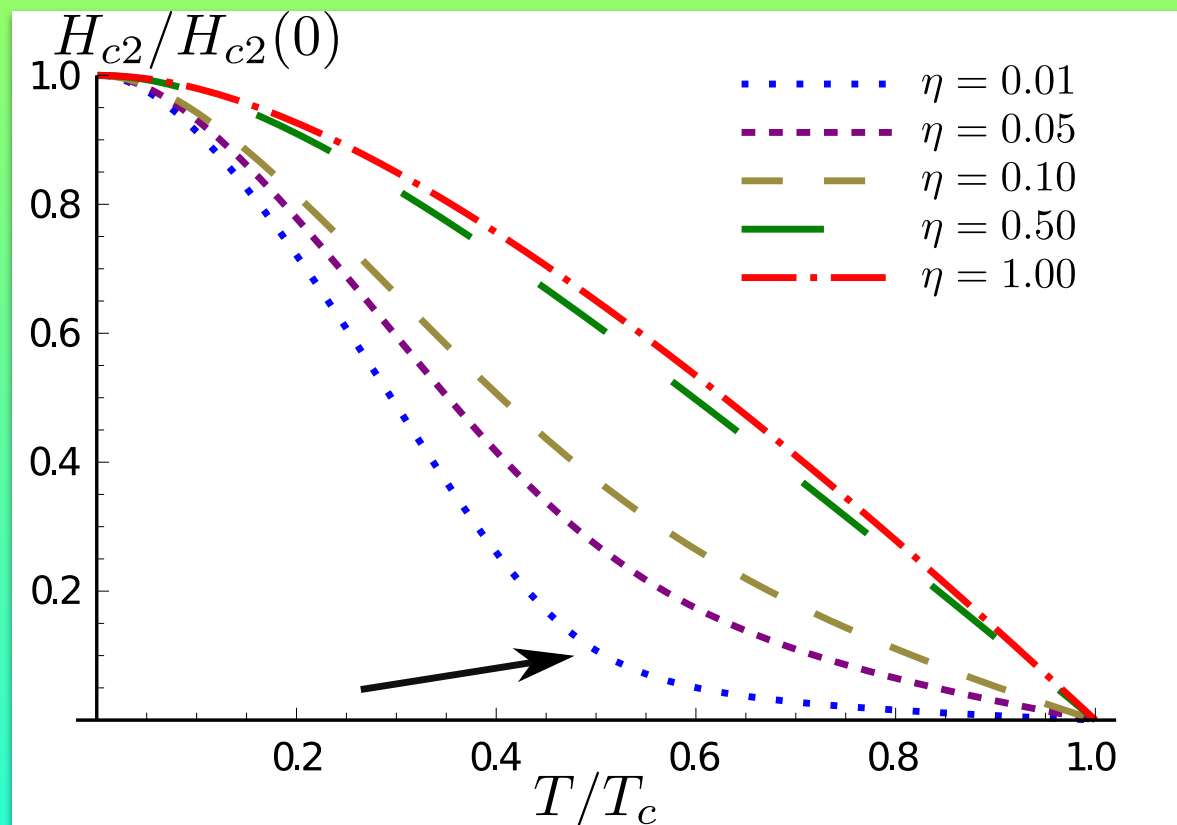
- Solving this equation gives pairs (H, T) and since $T = T_c$ (linearised equations) we get pairs (H_{c2}, T_c) .

Results for H_{c2}

JME & Balatsky, arXiv:1401.5318

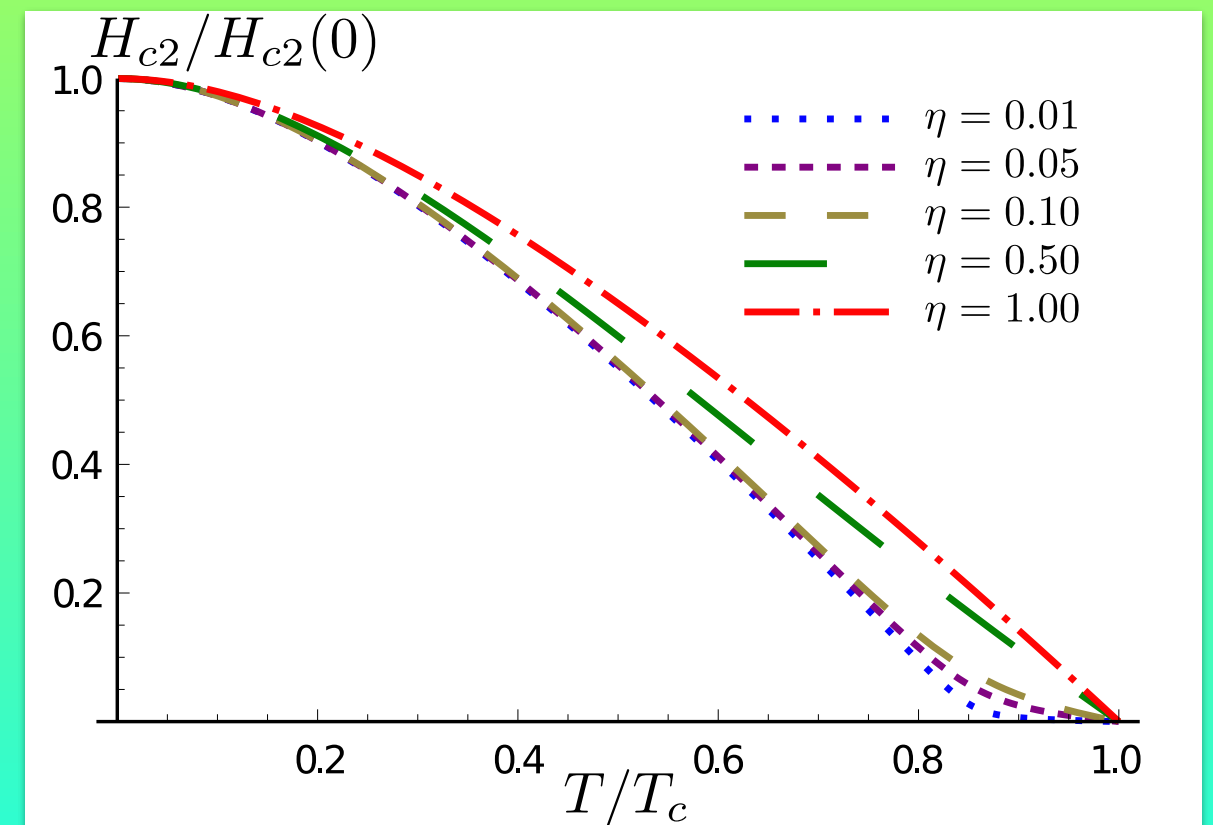
Solve for two sets of parameters:

$$\eta = D_2/D_1$$



Parameters: Fernandes, PRB 2013

$$\lambda_{11} = 0.14, \lambda_{22} = 0.13, \lambda_{12} = 0.02$$

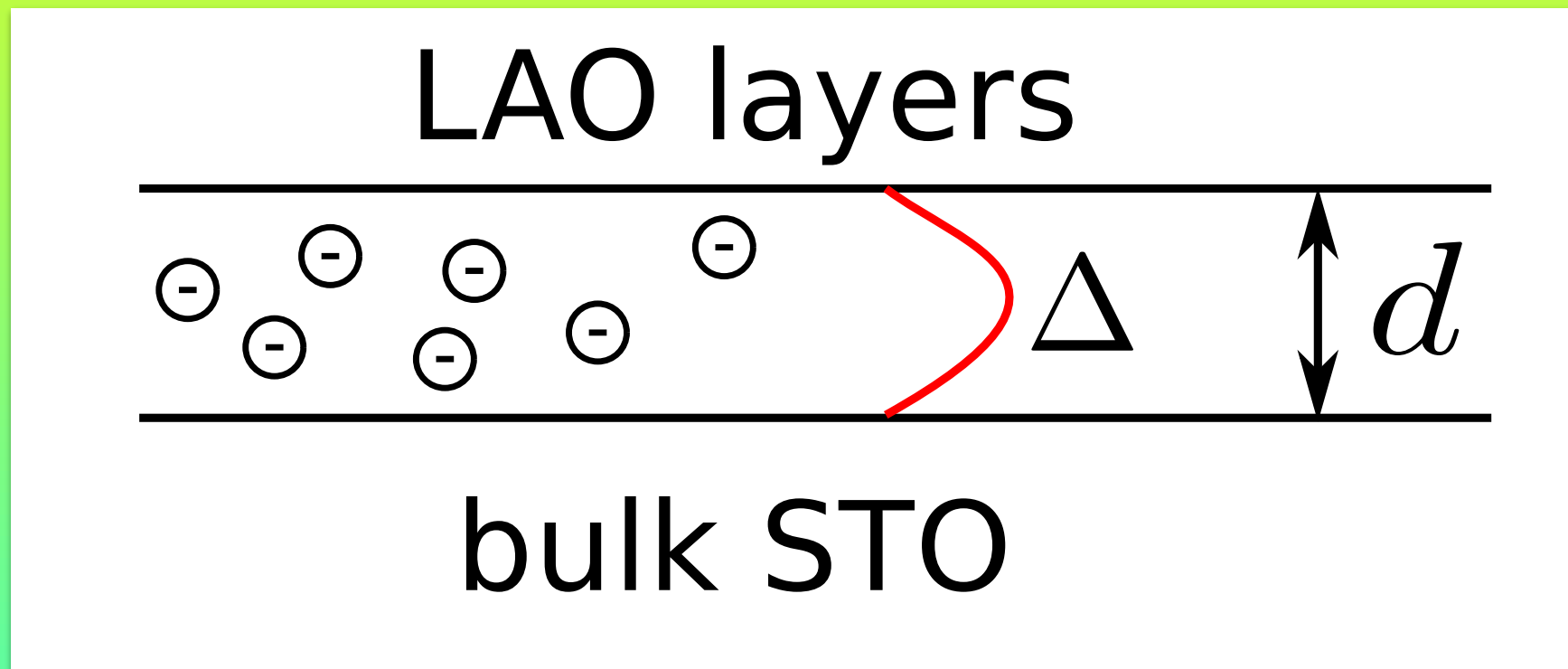


Parameters: Bussmann-Holder, Ferroelectrics 2010

$$\lambda_{11} = 0.3, \lambda_{22} = 0.1, \lambda_{12} = 0.015$$

Interface system

Thin superconducting layer



- retain ∇_z term in the Usadel equation
- Incorporate the effects of Rashba spin-orbit coupling

Finite thickness

- need to retain ∇_z term in

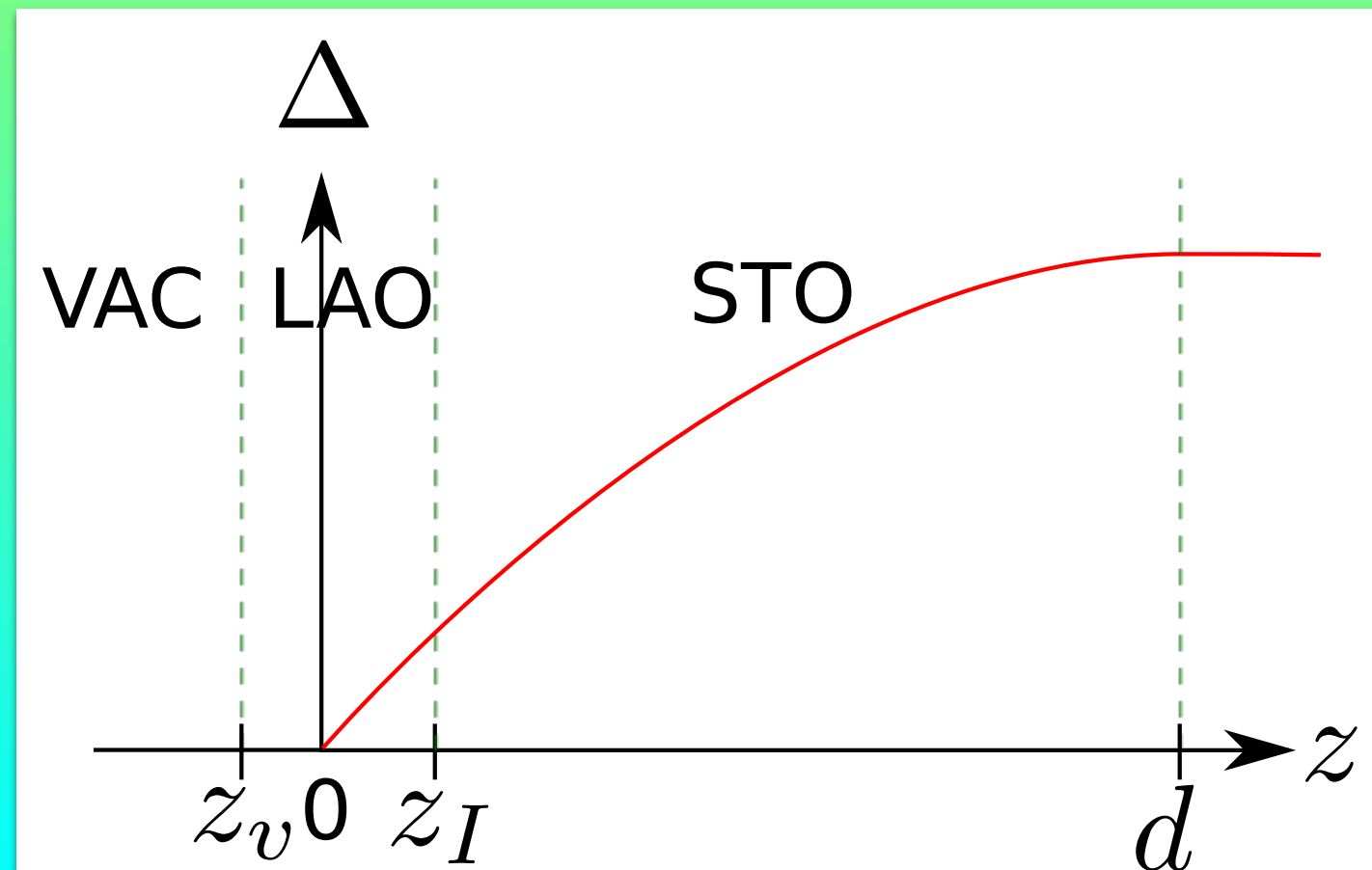
$$2\omega f_m - D_m \left(\nabla_x^2 + \nabla_z^2 - \frac{4\pi^2 H^2 x^2}{\phi_0^2} \right) f_m = 2\Delta_m$$

- At the boundary to the vacuum, $\Delta = 0$
- At an interface between a SC and a metal $\frac{d\Delta}{dz} = 0$

- thickness: $d \sim 12$ nm

- $\nabla_z^2 \rightarrow -\frac{\pi^2}{4d^2}$

- Incur an extra energy cost: effectively H increases

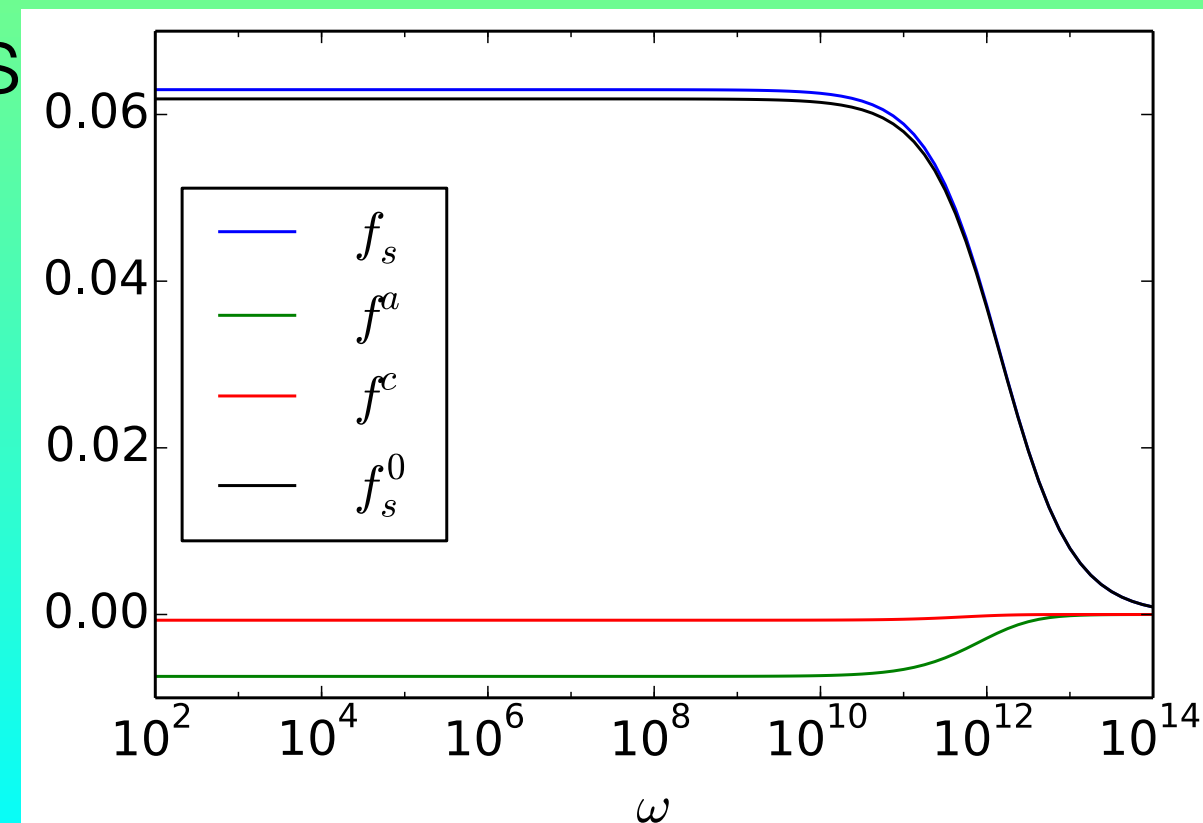


Spin-orbit coupling (SOC) at the interface

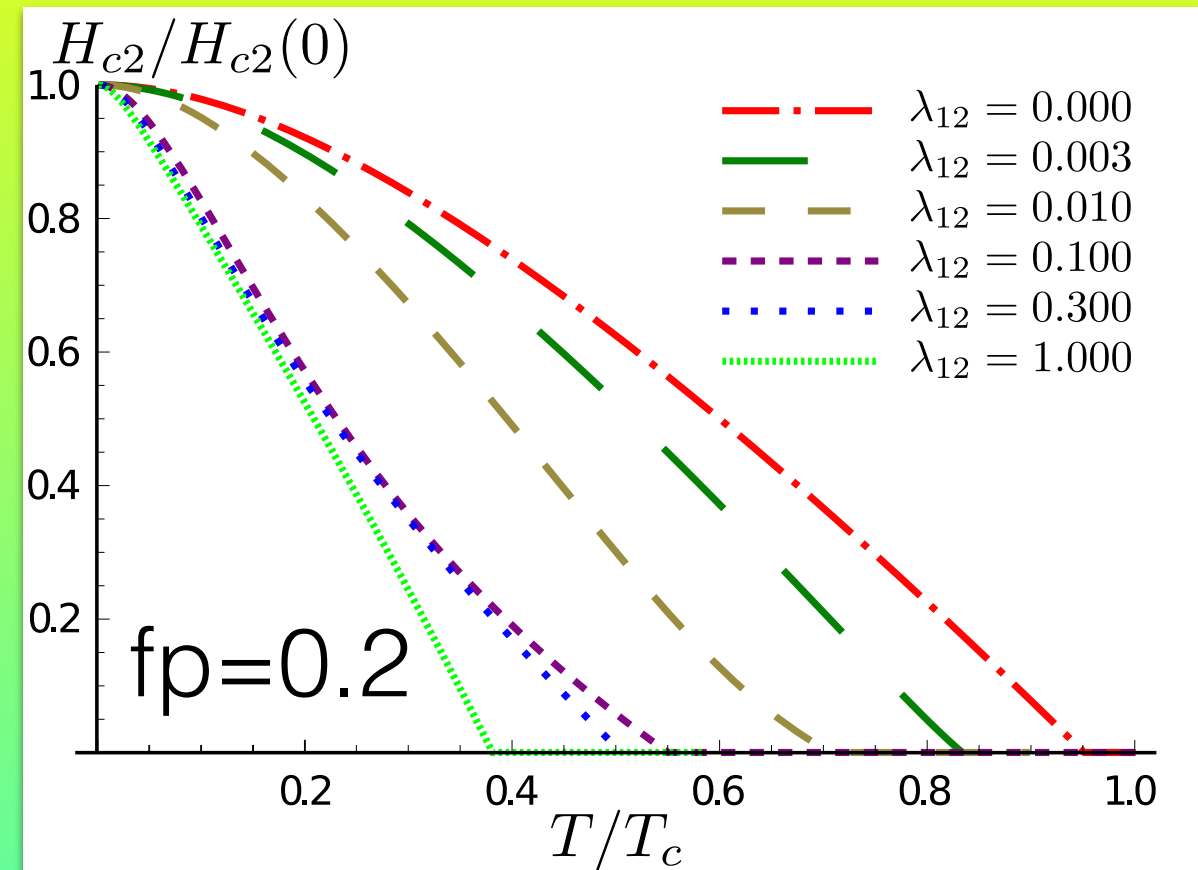
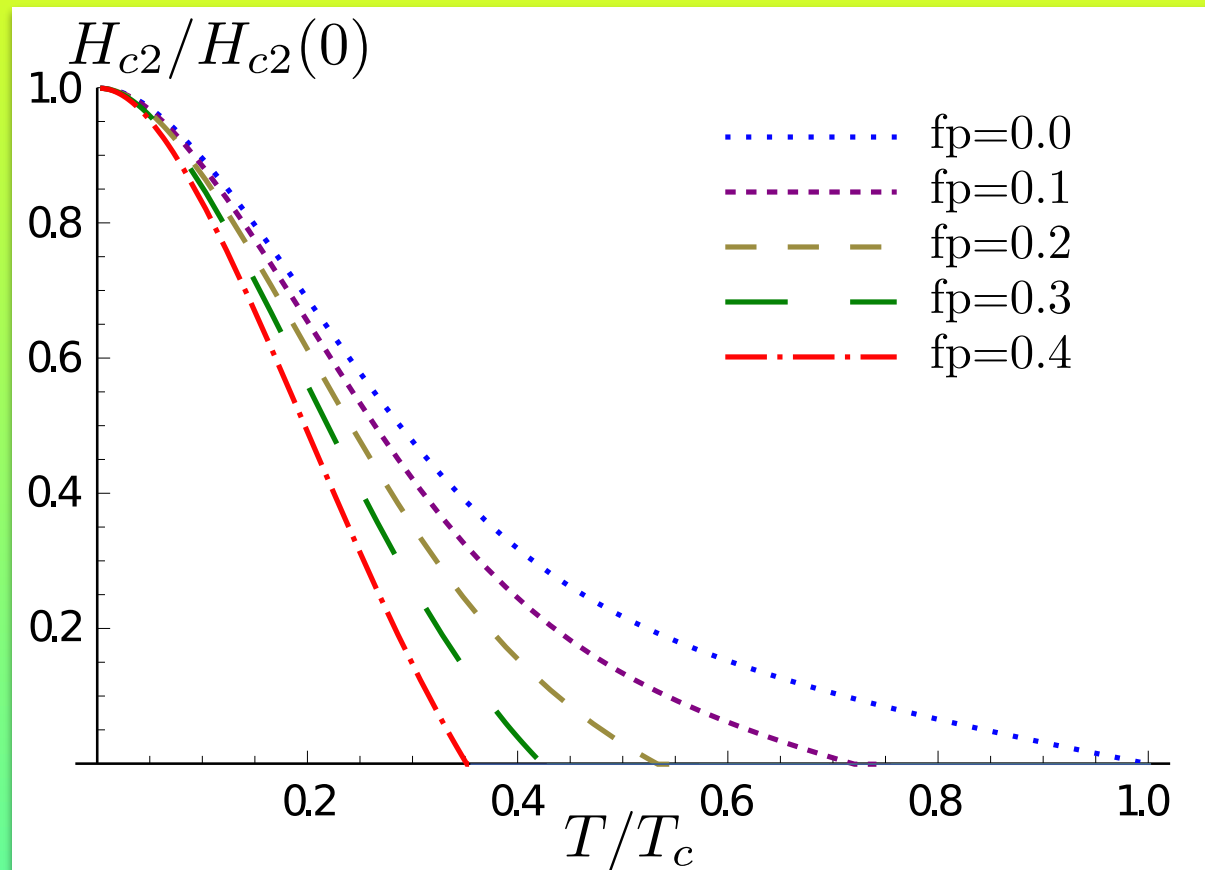
- Due to inversion symmetry breaking get strong Rashba SOC
- Leads to a modification of the momentum operator, anomalous Green's function f becomes a matrix

$$\nabla_x f \rightarrow \nabla_x f + \frac{i\alpha m_e}{\hbar} [\sigma_y, f] \quad \alpha : \text{SOC coupling strength}$$

- singlet and triplet components of f get coupled
- Concentrate on dominant singlet component
- singlet f gets energy penalty

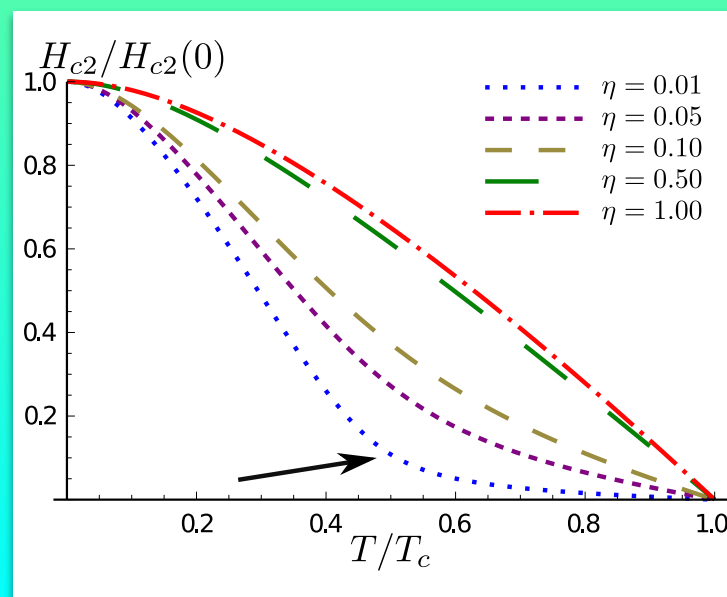


LAO/STO results



$$\lambda_{11} = 0.14, \lambda_{22} = 0.13, \lambda_{12} = 0.02$$

Comparison:
bulk STO
results

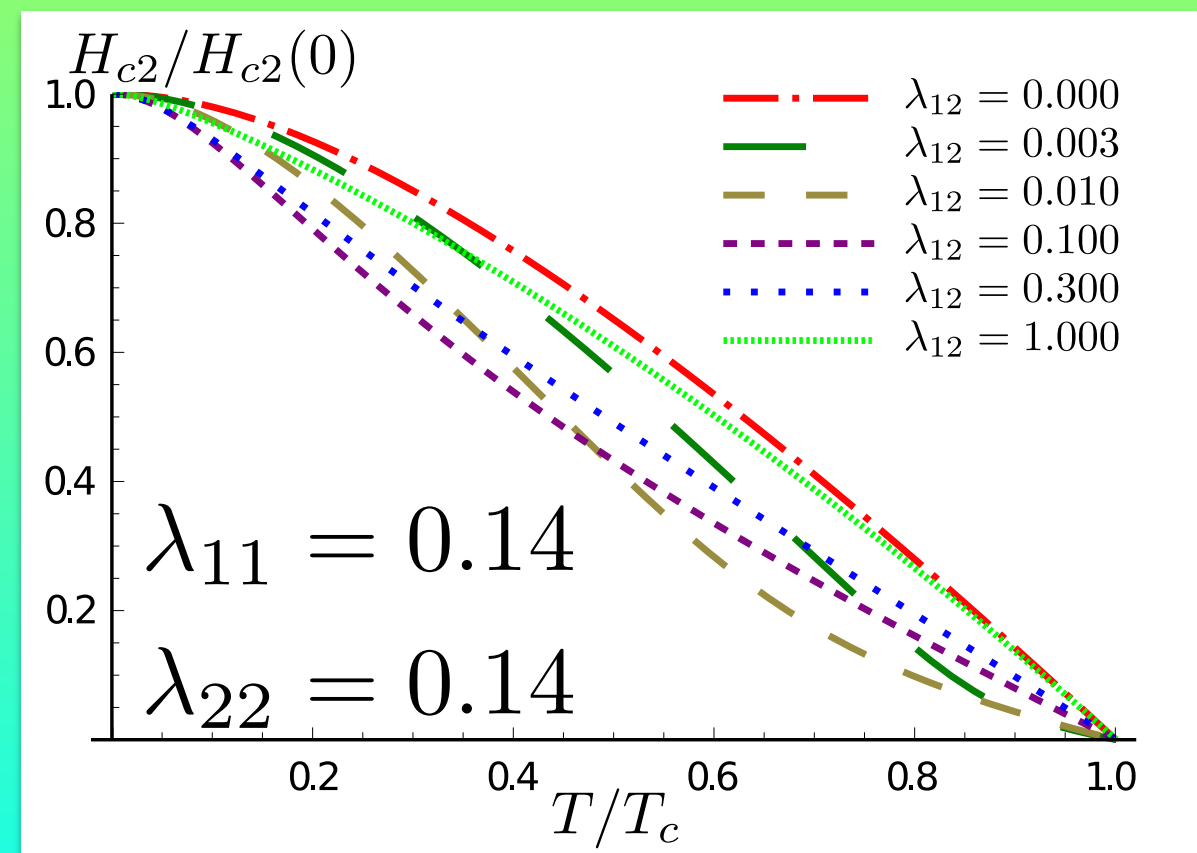
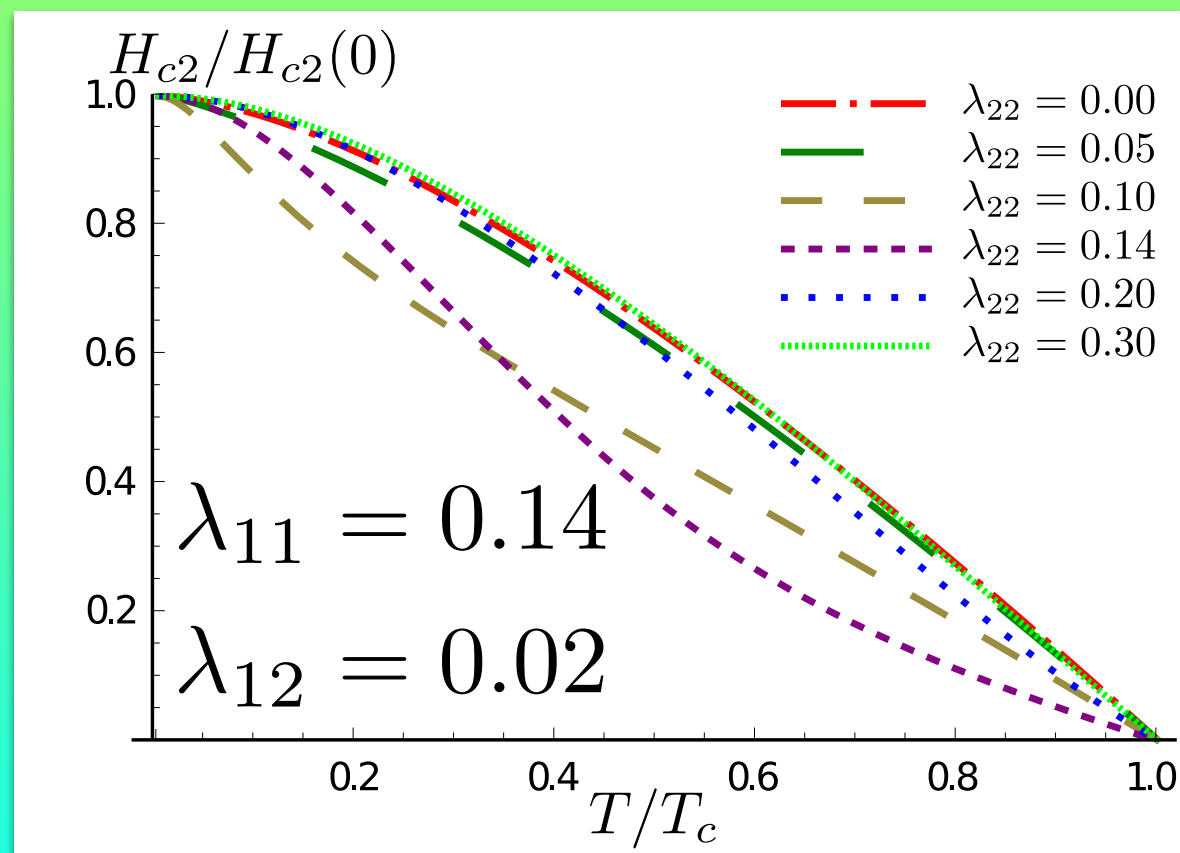


Conditions under which H_{c2} is a useful probe

H_{c2} is useful when

- $\lambda_{11} \approx \lambda_{22}$

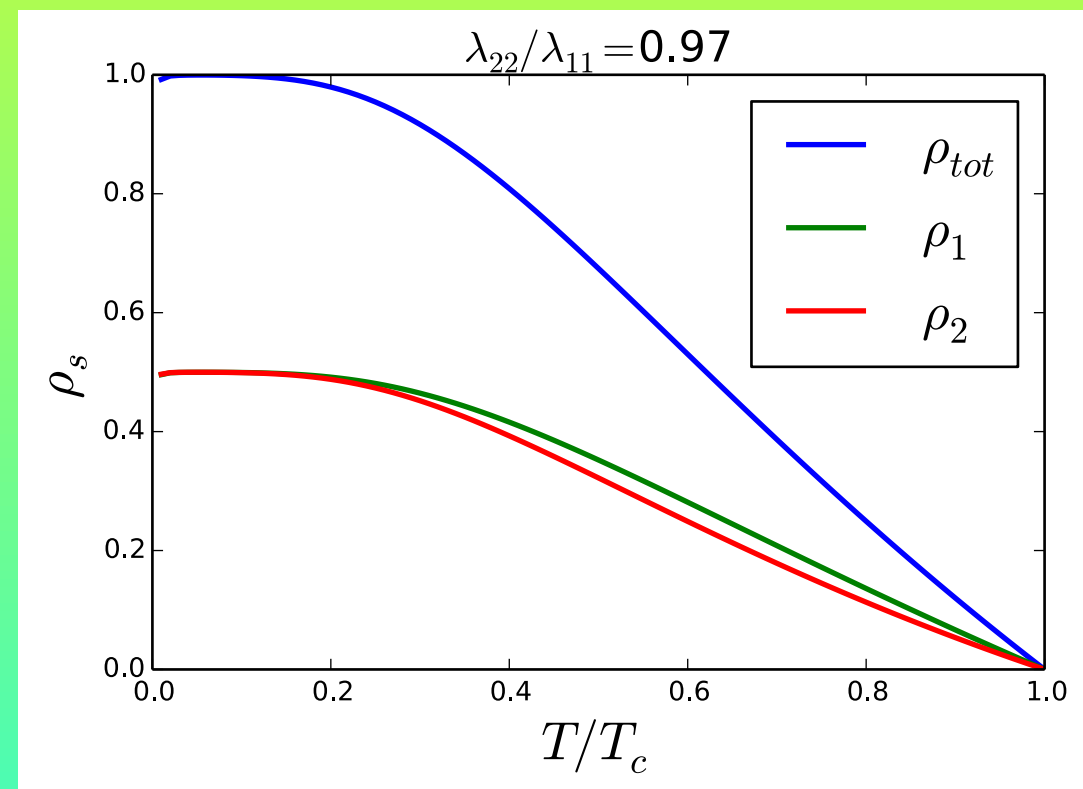
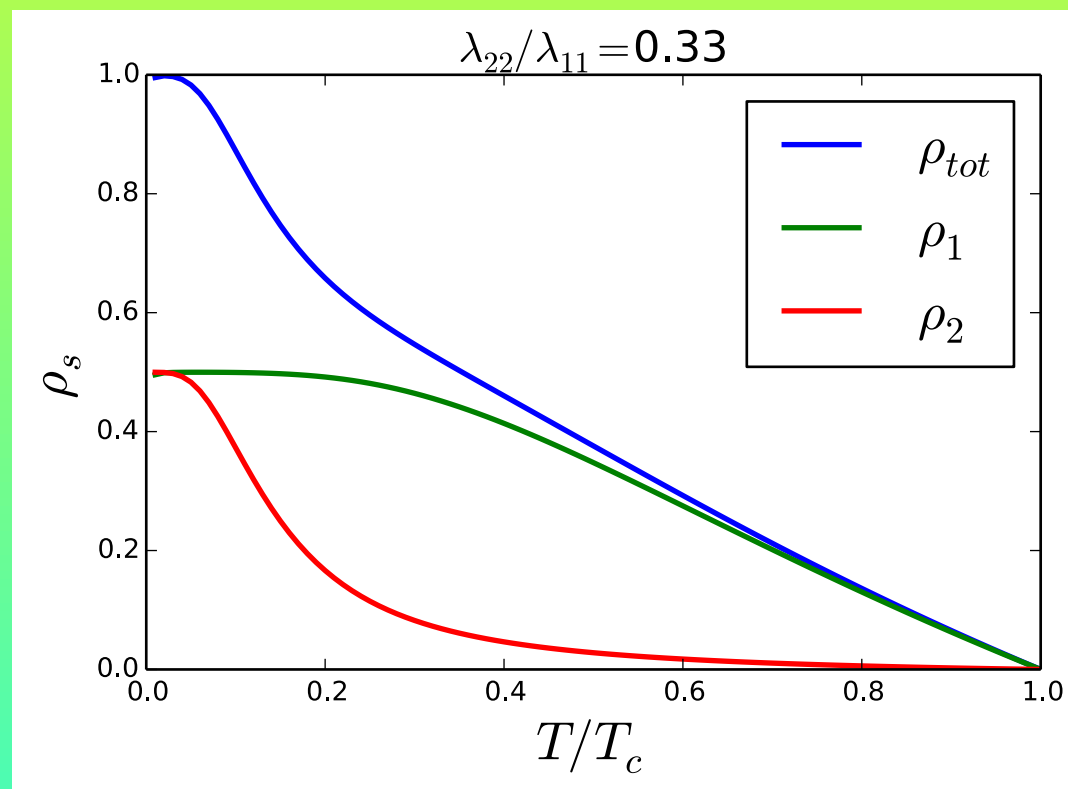
$$\lambda_{12} \ll \lambda_{11}$$



$$\eta = \frac{D_2}{D_1} = 0.1$$

Hc2 and superfluid density are complementary probes

- Superfluid density useful when: $\lambda_{11} \gg \lambda_{22}$

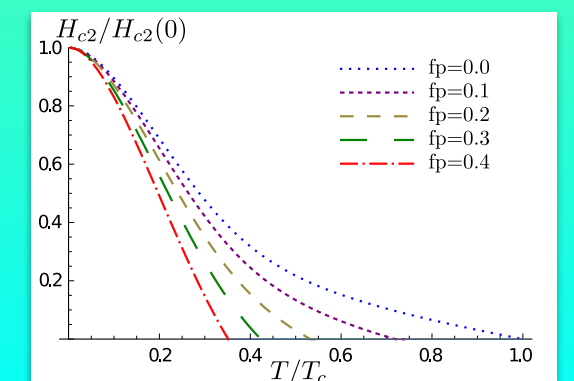
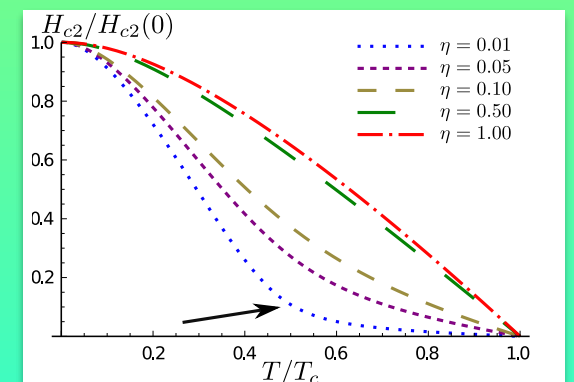
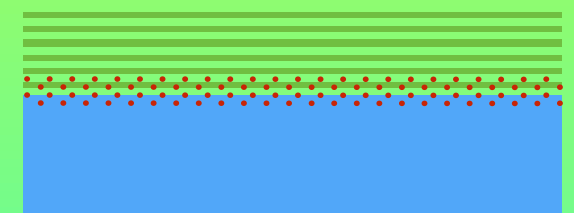
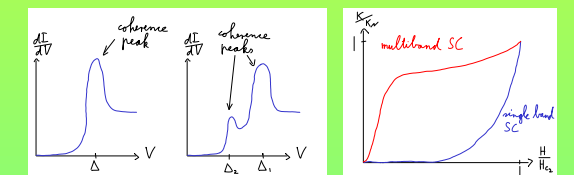
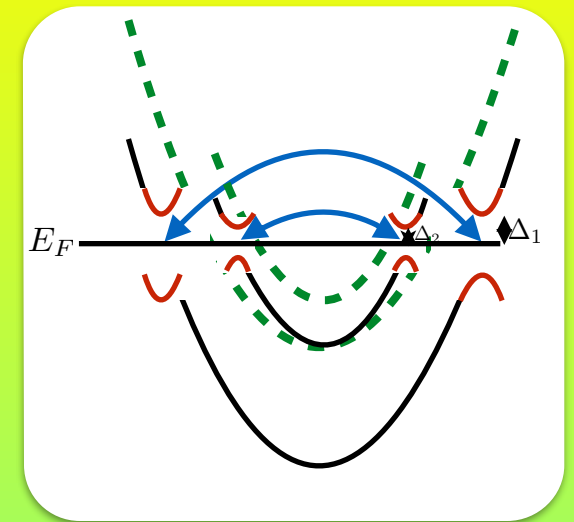


following Kogan, PRB 2009

- Upper critical field Hc2 useful when: $\lambda_{11} \approx \lambda_{22}$
measure onset of SC

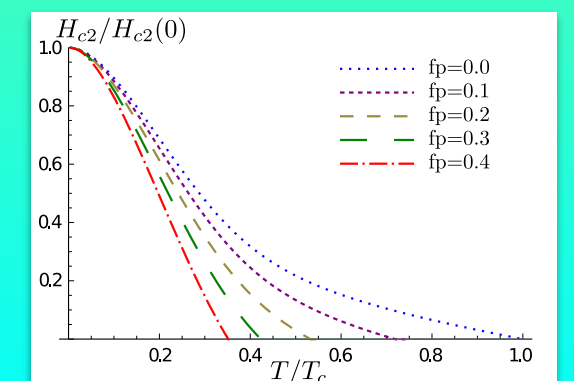
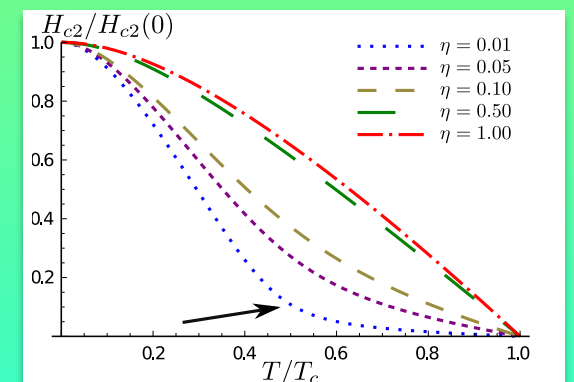
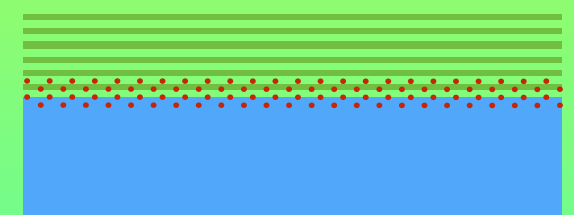
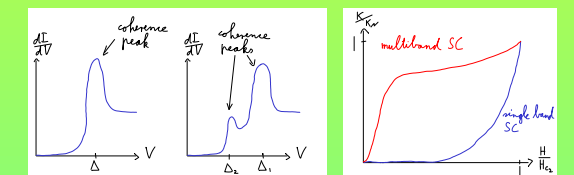
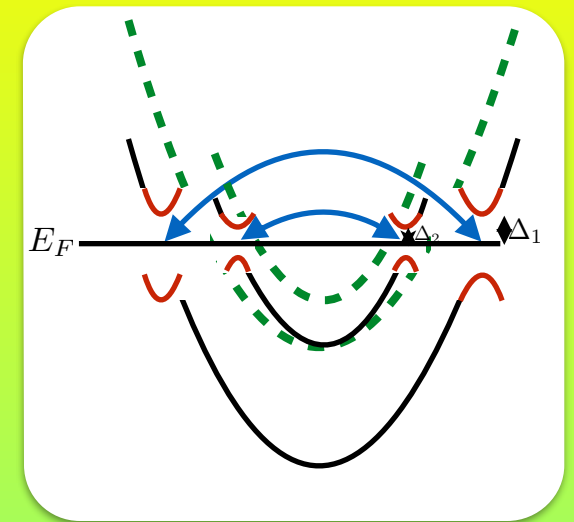
Summary

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- Various techniques for detecting MBSC
- LAO/STO interface: metallic layer
- Upper critical field H_{c2} : Probe for multiband superconductivity - applicable to bulk and interface
- SF density and H_{c2} are complimentary probes



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Thank you!